Molecular structure, glass transition temperature variation, agglomeration theory, and network connectivity of binary P-Se glasses

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Raman scattering and $^{31}$P NMR results show that the backbone of binary P$_x$Se$_{1-x}$ glasses is composed of Se$_x$-chain fragments, pyramidal $P(Se_{1/2})_3$ units, quasitetrahedral Se = $P(Se_{1/2})_3$ units, and ethylenelike $P_2(Se_{1/2})_4$ units at low P content ($x<0.47$). Concentrations of the various building blocks independently established from each spectroscopic probe are found to be correlated. Theoretical predictions for the glass transition variation $T_g(x)$ from agglomeration theory are compared to the observed $T_g(x)$ trends established from temperature-modulated differential scanning calorimetry. The comparison shows that a stochastic network description is an appropriate one of glasses at low $x$ ($x<0.12$). At medium $x$ ($0.12<x<0.47$), substantial medium-range structure evolves in the form of polymeric ethylenelike units that comprise elements of the barely rigid backbone. At higher $x$ ($x>0.47$), a rapid phase separation of monomeric P$_3$Se$_3$ units from the backbone takes place, leading to a molecular glass with a rather low $T_g$ at $x>0.50$.

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I. INTRODUCTION

Bulk glass formation in the P$_x$Se$_{1-x}$ binary occurs over wide compositions 4 $0<x<0.80$, with a narrow window 0.52 $<x<0.60$ centered at $x=0.57$ corresponding to the P$_3$Se$_3$ stoichiometry across which melts display a propensity to crystallization rather than glass formation. Melts in the window usually form molecular solids composed of P$_4$Se$_3$ monomers. The monomer consists of a triangular P$_3$Se$_3$ prism capped by a pyramidal P(Se$_{1/2}$)$_3$ unit (Fig. 1). As a solid, P$_3$Se$_3$ exists in two ordered ($\alpha, \alpha'$) low-$T$ phases and two orientationally disordered ($\beta, \gamma$) phases prior to melting at 244 °C. Transformations between these polymorphs have also been studied. The variety of building blocks occurring in the present binary are illustrated in Fig. 1, including the P$_4$Se$_3$ monomer structures in the $\alpha$ and $\beta$ phases. Upon melting $\beta$-P$_3$Se$_3$, melts possessing a polymeric structure are formed and consist of ethylenelike $P_2(Se_{1/2})_4$ units. Such structures apparently constitute an important part of the backbone of binary P-Se glasses in the 0.20 $<x<0.50$ range, as will become transparent later.

The molecular structure of the Se-rich (0 $<x<0.52$) and P-rich (0.60 $<x<0.80$) glasses has been the subject of previous investigations by differential scanning calorimetry, Raman scattering, and solid-state NMR. $^{11,12}$ $^{31}$P NMR chemical shifts of these building blocks have been established. $^{13}$ Raman scattering provides a powerful complementary probe to establish details of glass structure. Because of the diversity and complexity of glass structure and Raman lineshapes, particularly at $x<0.50$, deconvolution of Raman line shapes and microscopic identification of vibrational modes have been a challenge.

In this work we have examined Se-rich glasses (0 $<x<0.52$) in Raman scattering and $^{31}$P NMR measurements. Raman and NMR results on the crystalline reference com-

FIG. 1. Local building blocks of the P-Se glass system.
pounds $P_xSe_3$ and $P_xSe_4$ have served as an important aid in mode and site assignments, permitting us to decode the structure of these glasses on an atomic level. In addition to pyramidal $P(Se_{1/2})_3$ units, our experiments show that polymeric ethylenelike $P_2(Se_{1/2})_4$ units and quasi-tetrahedral $Se=P(Se_{1/2})_3$ units also occur in the Se-rich glasses ($x$ $<$ 0.50). Glass transition temperatures ($T_g$) are studied$^{14}$ by temperature-modulated differential scanning calorimetry (MDSC). The observed $T_g(x)$ variation is analyzed in terms of glass structure results using agglomeration theory.$^{15}$ As we will demonstrate, this analysis shows that the $T_g(x)$ variation serves as a good measure of network connectivity, and at low $x$ ($<$0.12), the agglomeration of the network is stochastic in character.

II. EXPERIMENTAL RESULTS

A. Sample synthesis

$P_xSe_{1-x}$ glasses in the $0<x<0.52$ composition range were synthesized using 99.999% Se and P lumps as starting materials from Cerac Inc. The elements were handled in a glove bag purged with dry-$N_2$ gas and reacted at $650^\circ C$ for at least 72 h in evacuated ($2 \times 10^{-7}$ Torr) quartz ampoules. After equilibrating the samples at $400^\circ C$, the ampoules were water quenched to realize micaceous glass samples with colors ranging from black to reddish brown as the P content increased to $x=0.50$.

Samples of $c-P_xSe_3$ were prepared by reacting the elements in the desired ratio and slow cooling the melt. Samples of $c-P_xSe_4$ were synthesized by reacting an intimate finely ground mixture of $c-P_xSe_3$ and elemental Se in the stoichiometric ratio, and heating at $330^\circ C$ for 72 h. Two glass samples were prepared from this material upon heating to its melting temperature ($T_m=340^\circ C$) for a short time (90 min) and an extended period (3 h), respectively. These samples were examined by Raman scattering and $^{31}$P NMR and revealed striking differences in molecular structure as will be discussed later.

B. Thermal characterization

We used a model 2920 temperature-modulated DSC from TA Instruments, Inc. to establish the glass transition temperatures ($T_g$'s) of the $P_xSe_{1-x}$ glasses. A heating rate of $3^\circ C/\text{min}$ and a modulation rate of $1^\circ C/100$ s were used for all scans. Scans were made both increasing in $T$ past $T_g$ and decreasing in $T$ from $T_g$. The inflection point of the total heat flow endotherm was taken as $T_g^{app}$, while that of the reversing heat flow endotherm was taken as $T_g$. In general, $T_g^s>T_g^{app}$ because of the presence of a kinetic heat flow, also called the nonreversing heat flow ($\Delta H_m$), as a precursor to the actual glass transition.

Figure 2(a) shows a summary of $T_g(x)$ variation in the present glasses. Figure 2(b) compares the present $T_g^{app}(x)$ with the published$^{16}$ glass transitions on the present binary glasses from previous work using DSC. In Fig. 2(b), in each instance, one is comparing the glass transition temperature deduced from the total heat flow, one using an MDSC, and all others using DSC instruments. The agreement between various results is reasonable. A noteworthy feature of the $T_g(x)$ trend in Fig. 2(a) is its smoothness and almost flat variation with $x$ in the 0.20 $<$ $x$ $<$ 0.45 range, followed by a steep increase at $x$ $>$ 0.45. On the other hand, the $T_g^{app}$ trend provides some evidence of a discontinuity near $x$ = 0.30, a feature also noted by previous workers.$^8$ The latter is an artifact resulting from the use of the total heat flow to extract $T_g$'s ($T_g^{app}$). Shifts in $T_g^{app}$ result due to kinetic effects associated with nonreversing heat flow term. Such shifts are nearly eliminated when $T_g$'s are extracted from the reversing heat flow term [Fig. 2(a)].

C. Raman scattering

Raman-Stokes spectra of freshly fractured surfaces of the glasses were taken at room temperature using an Instruments SA model T64000 Raman facility, equipped with a triple monochromator, liquid-$N_2$-cooled charge-coupled device (CCD) detector and a microscope. Typically less than 1 mW of 647.1 nm radiation from a Kr+ ion laser was used to excite the scattering. Sample homogeneity was verified by comparing spectra on a 2-$\mu$m spatial resolution using a microscope attachment. We also recorded spectra of the glasses in the fused quartz ampoules used to synthesize them. Spectra of the samples taken in laboratory ambient looked iden-
tical to the ones recorded in quartz ampoules and further revealed no aging effects. All spectra reported here were taken at laboratory ambient.

Figures 3a and 3b reproduce observed Raman line shapes at selective compositions plotted as a function of P content, starting from pure Se (x=0), up to x=0.50. Starting from the Se-Se stretch modes at 250 cm$^{-1}$ (labeled II), one sees growth of features labeled I, III, and IV, which are, respectively, identified as modes of pyramidal $P(Se_{1/2})_3$ units, ethylenelike $P(Se_{1/2})_4$ units, and quasitetrahedral $P(Se_{1/2})_3 Se$ units of the backbone. At $x>0.40$ and in particular at $P_{0.50}Se_{0.50}$, the sharp feature labeled V in Fig. 3(b) is identified with appearances of $P_xSe_3$ monomer units in these P-rich glasses. Figure 4 plots the fractional area ratio $A_n/A(x)$ of various species $n=I-V$ as a function of P concentration $x$. The Raman line shapes were deconvoluted in terms of a superposition of Gaussians to obtain mode intensities ($I_n$), frequencies ($\nu_n$), and widths ($\Gamma_n$). All three variables were kept floating in the least-squares refinement. The areas are obtained by summing contributions of various Gaussians ascribed to a given building block (Table I). We shall return to discuss the justification for the proposed mode assignments (Table I) later.

Figure 5 reproduces Raman line shapes of P-Se glasses in the low-frequency region (160$<\nu<220$ cm$^{-1}$) and permits one to track growth of the 188 cm$^{-1}$ mode, which is identified with $P_x(Se_{1/2})_4$ units. These results show that $P_x(Se_{1/2})_4$ units are first nucleated in the glasses near $x=0.20$.

Figures 6(a) and 6(b) reproduce selective regions of the Raman line shapes of P-Se glasses at high P content where modes of $P_xSe_3$ monomeric units manifest at 132 and 482 cm$^{-1}$. A perusal of these line shapes shows that the monomer is first nucleated near $x=0.47$ in the glasses. Figure 7 shows spectra of $c-P_xSe_3$, $c-P_2Se_4$, and $g-P_2Se_4$. The spectrum of $c-P_2Se_4$ is in good agreement with earlier published reports. The spectrum of $g-P_2Se_4$ is dominated by the modes observed in $c-P_2Se_3$ and $c-P_2Se_4$. Raman peaks in the $P_4Se_4$ glass are in general broader in width than those observed in $c-P_2Se_4$. In addition, weaker features in the spectrum (in particular, the peak at 250 cm$^{-1}$) also reveal the presence of structural units richer in Se than the average glass composition.
D. $^{31}$P NMR spectroscopy and resonance assignments

$^{31}$P magic-angle spinning (MAS) NMR studies were carried out at 121.5 MHz on a Bruker CXP 300 spectrometer, equipped with a multinuclear 4-mm probe. Spectra were recorded on powdered samples, using 90° pulses of 4 μs length and relaxation delays of 10 min. Typical spinning frequencies were 15.1 kHz. Figure 8 shows representative $^{31}$P MAS NMR spectra of P-Se glasses in the 0.1, x, 0.4 concentration range. The results are in good agreement with previous work. At low x, spectra consist of two resonances near zero and 140 ppm, respectively, indicating the presence of two distinct P sites. The high-frequency resonance is assigned to pyramidal $^{3}$Se$_{1/2}$~31. This assignment is consistent with the $^{31}$P NMR chemical shifts measured on various crystalline model compounds bearing the $^{3}$Se$_{1/2}$~3 group. Furthermore, complementary spin-echo decay experiments reveal that in Se-rich glasses, x<0.20, no direct P-P bonds are detected to an appreciable extent. The resonance near zero ppm is assigned to tetrahedral Se=P($^{3}$Se$_{1/2}$)$_{3}$ units. This assignment is more difficult to justify because to date no crystalline model compounds are known, in which P is surrounded by three bridging and one terminal doubly bonded Se atom. Tetrahedrally coordinated PSe$_{4}$~3 groups do exist, however, in various ternary orthoselenophosphate compounds, and their $^{31}$P chemical shifts are generally found within the chemical shift range zero to ~100 ppm. Further support for the above assignment comes from the x dependence of the relative peak areas evident from Fig. 8: the experimental species concentrations of the Se=P($^{3}$Se$_{1/2}$)$_{3}$ units are in quantitative agreement with the corresponding values predicted from an equilibrium model (see below).
Closer inspection of Fig. 8 shows that the center of gravity of the high-frequency resonance is slightly shifted when $x \leq 0.20$. These changes in line shape suggest the appearance of new structural units at higher phosphorus concentrations.

Insights have emerged from $^{31}$P spin-echo experiments as previously discussed in detail, the homonuclear $^{31}$P-$^{31}$P dipole-dipole coupling strength can be quantified selectively using a $90^\circ-t_1-180^\circ-t_1$ Hahn spin-echo sequence by measuring the spin-echo intensity as a function of the evolution time $2t_1$. Since this dipolar interaction is rigorously dependent on the internuclear distance distribution, the experiment differentiates between P-bonded and non-P-bonded types of phosphorus species. This prediction has been verified previously by detailed simulation. The simulations assume that the multispin interaction can be analyzed as a sum of pairwise interactions, resulting in a superposition of oscillatory time dependences of spin-echo decay intensity, where the frequency components depend on the internuclear distances involved and on the orientation of the internuclear vector relative to the magnetic field direction. Following powder averaging, the simulations produce decays of normalized spin-echo intensity as a function of the evolution time $2t_1$, which are summarized in Fig. 9. Here circles show the simulated curves calculated with the assumption of a dominant $^{31}$P-$^{31}$P two-spin interaction, whereas the solid curves are Gaussian approximations to these spin-echo decay curves.

**FIG. 9.** Predicted $^{31}$P spin-echo decay intensity as a function of dipolar evolution time for P$_x$Se$_{1-x}$ glasses at $x = 0.10$, 0.25, and 0.40, respectively. Circles show the result of a rigorous calculation with a single dominant two-spin dipolar interaction, while solid lines represent the approximation of the decay as a Gaussian function. Left side: spin-echo decay for the ethylenelike P$_2$(Se$_{1/2}$)$_2$ units. Right side: spin-echo decay for P(Se$_{10}$)$_3$ units. For additional details see Ref. 18.
All of the computational details and further assumptions made in these simulations are given in Ref. 18. Figure 9 reveals that the spin-echo intensities for the $P_2(Se_{1/2})_4$ groups (having a strong dipolar interaction owing to the single P-P bond) decay much faster than those predicted for P atoms not involved in direct phosphorus-phosphorus bonding. From a deconvolution of the experimental spin-echo decays into these two distinct contributions, it is then possible to estimate fraction of P atoms involved in P-P bonding. This analysis\textsuperscript{18} reveals that P-P bonding starts making a significant contribution to the glass structure at P concentrations above 25 at.%. The quantitative assessment has shown, however, that the extent of P-P bonding is lower than that expected on the basis of merely statistical atomic linking. Assuming, therefore, that homopolar bonding is for the most part limited to one P-P bond per P, we identify this species with a $P_2(Se_{1/2})_4$ group. The results are in excellent accord with Raman scattering observation of a threshold at $x > 0.20$ for the nucleation of this bonding fragment in the glasses. The network structure derives from the crystal structure of polymeric $P_4Se_4$, which has recently been solved by Ruck.\textsuperscript{5} The $^{31}$P chemical shifts of c- and g-$P_4Se_4$ closely match each other, further supporting the important structural role played by the $P_2(Se_{1/2})_4$ units in this concentration region.

$^{31}$P MAS NMR spectra at $x > 0.47$ reveal two additional distinct resonances near 65 and $\sim 75$ ppm in an approximate area ratio of 1:3 (see Fig. 10). These resonances are unambiguously assigned to the apical and basal P atoms of $P_3Se_3$ monomers, a result in harmony with the Raman observation of a threshold composition $x > 0.47$ for the appearance of the monomer in the glasses. Figure 10 illustrates that the concentration of these units can be influenced by the thermal history of the glass. Here the $^{31}$P MAS NMR spectra of a glass at $x = 0.50$ prepared by melting c-$P_4Se_4$ for the duration of 12 h at 350 °C (equilibrated melt) and independently a second sample for 90 min at 340 °C (nonequilibrated melt) are compared: peak integration reveals that upon equilibrating melts by an extended heating contribution of monomeric $P_3Se_3$ units in the glass increases from 18% to 34%. Both the Raman linewidths and NMR widths associated with $P_3Se_3$ species are quite narrow and suggest that the underlying molecular unit is decoupled from the glass backbone; i.e., it is monomeric in nature. The intrinsic value of these results on a nonequilibrated melt is that they serve as an important check on our Raman mode and P NMR site assignments in the glasses.

**III. DISCUSSION**

Some of the issues we will discuss in this section include Raman mode assignments, evolution of glass molecular structure, agglomeration theory and $T_g(x)$ variation, and its consequences on network connectivity.

**A. Raman mode assignments**

In Table I we have summarized the proposed assignment of modes. In the following we provide some justification for these assignments and, in select cases, the eigenvectors.

**FIG. 10.** Effect of thermal history on the $^{31}$P MAS NMR spectra (a) and (b) and Raman spectra (c) of $P_{0.5}Se_{0.5}$ glass. (a) NMR glass prepared by melting crystalline $P_4Se_4$ at 350 °C for 12 h. (b) NMR of glass prepared by melting crystalline $P_4Se_4$ at 340 °C for 90 min. (c) Raman spectra of corresponding samples.
TABLE I. Raman mode assignments.

<table>
<thead>
<tr>
<th>Mode frequency (cm$^{-1}$)</th>
<th>Local unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>I 210, 330</td>
<td>P(Se$_{1/2}$)$_3$ pyramidal units</td>
</tr>
<tr>
<td>II 237, 250</td>
<td>Se chains and rings</td>
</tr>
<tr>
<td>III 180, 330, 350, 370</td>
<td>P$<em>2$(Se$</em>{1/2}$)$_2$ ethylene like units</td>
</tr>
<tr>
<td>IV 510</td>
<td>Se=P(Se$_{1/2}$)$_3$ quasi tetrahedral units</td>
</tr>
<tr>
<td>V Narrow modes at 184,</td>
<td>Modes of P$_2$Se$_3$ monomer</td>
</tr>
<tr>
<td>212, 320, 371, 1483</td>
<td></td>
</tr>
</tbody>
</table>

1. Group I modes: \( \text{P(Se}_{1/2}\text{)}_3 \text{ pyramidal units} \)

The pair of modes at 210 and 330 cm$^{-1}$ in the Raman spectra of the glasses are identified with a pyramidal \( \text{P(Se}_{1/2}\text{)}_3 \) unit and are labeled I in Table I. The eigenvectors of the 330-cm$^{-1}$ mode represent a symmetric breathing of the three Se atoms with the P-cation stationary. The 210-cm$^{-1}$ mode represents an asymmetric stretch of the unit in which the displacement of the P cation is nearly opposite to that of the three Se neighboring anions. These modes are also observed in Raman spectra of \( \text{c-P}_4\text{Se}_3 \) moieties and have been labeled as \( \nu_3 \) and \( \nu_4 \), respectively, in Ref. 10.

2. Group II modes: \( \text{Se}_n \text{ chain units} \)

The strongly Raman-active band observed near 250 cm$^{-1}$ in the present glasses is traced to a Se-Se stretch in \( \text{Se}_n \) chains fragments of Se glass. The band is asymmetric and has a lower-frequency companion at 237 cm$^{-1}$ in a Se glass, a feature that apparently persists upon P alloying. We identify band II in Table I as signature of \( \text{Se}_n \)-chain fragments in the binary glasses.

3. Group III modes: \( \text{P}_2\text{(Se}_{1/2}\text{)}_2 \text{ polymeric units} \)

The set of modes at 180, 330, 350, 370 cm$^{-1}$ and some weaker ones in between 310 and 340 cm$^{-1}$ are collectively labeled as III in Table I and are identified with the presence of a polymeric network made up of ethylenelike \( \text{P}_2\text{(Se}_{1/2}\text{)}_2 \) units. Support for such identification comes from the Raman scattering results of \( \text{c-P}_4\text{Se}_3 \) and \( \text{g-P}_3\text{Se}_4 \) shown in Fig. 7. The glass obtained by melting the crystal has essentially all the principal modes seen in the crystal, except that they are broadened.

4. Group IV modes: \( \text{Se}=\text{P(Se}_{1/2}\text{)}_3 \text{ units} \)

Although it may be tempting to assign the weak scattering at 510 cm$^{-1}$ to second-order scattering from Se$_n$ chains, the observed trends in scattering strength at 510 cm$^{-1}$ suggest otherwise. The latter shows a maximum at about \( x=0.20 \) and is thus uncorrelated to the monotonic decrease in concentration of Se$_n$ chains in the glasses with increasing \( x \). The mode at 510 cm$^{-1}$ is identified with a quasi tetrahedral \( \text{P(Se}_{1/2}\text{)}_3 \text{Se unit} \). A mode at 537 cm$^{-1}$ is observed in some samples of \( \text{P}_2\text{Se}_4 \) and has been identified with the presence of \( \text{P}=\text{Se} \) stretch. The molecular configuration in question is considered to isomerize to the \( \beta\)-\( \text{P}_2\text{Se}_4 \) form.

FIG. 11. Indicated species concentrations in P-Se glasses as deduced from NMR spectroscopy: A: Se-Se bonds, B: \( \text{P(Se}_{1/2}\text{)}_3 \text{ units} \), C: \( \text{Se}=\text{P(Se}_{1/2}\text{)}_3 \text{ units} \), D: \( \text{P}_2\text{(Se}_{1/2}\text{)}_3 \text{ units} \). For additional details, see Ref. 18.

5. Group V modes: \( \text{P}_4\text{Se}_3 \text{ monomer units} \)

The sharp peaks appearing at 184, 212, 370, and 483 cm$^{-1}$ labeled collectively as V in Raman spectra of a glass at \( x=0.50 \) identify the \( \text{P}_4\text{Se}_3 \) monomer. These modes have been previously assigned to \( \nu_6 \), \( \nu_4 \), \( \nu_2 \), and \( \nu_1 \) vibrations from a normal mode analysis of the monomer in Ref. 21. There is a weakly excited mode at 320 cm$^{-1}$, labeled as \( \nu_4 \), which overlaps with a mode of the \( \text{P}_2\text{(Se}_{1/2}\text{)}_3 \) units (group III).

B. Glass structure evolution with P content

Both Raman scattering (Fig. 4) and the $^{31}\text{P}$ NMR (Fig. 11) results independently provide the type and concentration of building blocks in the present glasses. The correlation between the details of glass structure between the two spectroscopies is rather comforting (Figs. 4 and 11). In Raman scattering, the richness of observed line shapes provides a means to directly resolve contributions of various building blocks of the network and, in particular, establish specific concentrations where a given building block is first nucleated in the glasses. A disadvantage of the method is that since the observed mode cross sections are never identical, the observed scattering strengths (Fig. 4) can currently only serve as a qualitative measure of concentrations of various species.

Fortunately, the $^{31}\text{P}$ NMR results are, on the other hand, inherently more quantitative. But these experiments do require a combination of measurements to deduce the concentrations of the various units as we discuss below. The spin-echo experiments allow quantification of the \( \text{P}_2\text{(Se}_{1/2}\text{)}_3 \) units, while the MAS NMR spectra serve to quantify the \( \text{Se}=\text{P(Se}_{1/2}\text{)}_3 \) groups. All of the P atoms remaining at each glass composition are then attributed to \( \text{P(Se}_{1/2}\text{)}_3 \) units. Furthermore, by comparing the concentrations with glass compositions, the number of Se-Se bonds can be deduced (Fig. 11). As expected, Se-rich moieties dominate at low P content, whereas the P-bonded species become dominant at \( x>0.35 \), in harmony with the Raman scattering results (Fig. 4). The
concentration dependence on glass composition is monotonic, and in particular no discontinuity is observed near $x = 0.40$, where a rapid change in $T_g$ is observed (Fig. 2).

The formation of $\text{Se}=\text{P(Se$_{1/2}$)$_3$}$ groups in the present glasses is of particular interest because, to date, this moiety is unknown in the crystal chemistry of phosphorus selenides. In particular, this unit is not present in the molecular structure of $\text{P$_5$Se$_5$}$ recently deduced by Blachnik and co-workers.\(^{24}\) Unlike the situation in the stoichiometrically analogous phosphorus oxide and sulfide, the structure of monomeric $\text{P$_2$Se$_3$}$ is based on two $\text{P(Se$_{1/2}$)$_3$}$ units which are connected to each other by bridging selenium atoms and by two diselenide bridges.

Results of Figs. 4 and 11 show that the concentration of $\text{Se}=\text{P(Se$_{1/2}$)$_3$}$ reaches its maximum value near $x = 0.2$. The concentration dependence of the $\text{Se}=\text{P(Se$_{1/2}$)$_3$}$ species on $x$ can be modeled quantitatively by assuming the presence of an equilibrium

$$\text{P(Se$_{1/2}$)$_3$} + \text{Se} \rightarrow \text{P(Se$_{1/2}$)$_3$}, \tag{1}$$

characterized by an equilibrium constant $K_T$ in the vicinity of 0.8.\(^{13,18}\) This equilibrium is operative in the molten state and is arrested permanently at $T_g$. Studies in melts ($T > T_g$) have further shown that this equilibrium shifts significantly towards the left as the temperature is increased.\(^{23}\)

At higher $P$-content, the glass structure is dominated by the three-fold-coordinated $\text{P(Se$_{1/2}$)$_3$}$ and $\text{P$_5$Se$_5$}$ species. Figure 11 also shows that a maximum in the concentration of $\text{P(Se$_{1/2}$)$_3$}$ units is reached near $x = 0.35$; at higher $P$ content, the $\text{P$_5$Se$_5$}$ species dominate. Again, these two three-coordinated species can be viewed as being connected by an equilibrium process of the form

$$\text{P$_5$Se$_5$} + \text{Se} \rightarrow 2\text{P(Se$_{1/2}$)$_3$}, \tag{2}$$

In the case of this equilibrium, however, high-$T$ NMR studies\(^{27}\) do not reveal any significant $T$ dependence. $\text{P$_5$Se$_5$}$ monomers make a significant contribution to the glass structure only at $x > 0.47$ as also revealed by the Raman results of Figs. 6(a) and 6(b). As Fig. 10 illustrates, the concentration of these units is strongly dependent on the thermal history. Related observations have been made in recent high-$T$ liquid-state \(^{31}P$ NMR studies of $\text{P-Se}$ melt containing 48 at.\% phosphorus.\(^{25}\) Furthermore, these liquid-state NMR experiments have also revealed that, although no molecular $\text{P$_5$Se$_5$}$ is detected in the glassy state at $x < 0.47$, these species are formed at high temperatures in $\text{P-Se}$ melts with $x$ values as low as 0.40. Systematic $T$-dependent studies reveal the presence of a melt depolymerization equilibrium of the kind

$$3\text{P$_5$Se$_5$} \rightarrow \text{P$_4$Se$_7$} + 2\text{P(Se$_{1/2}$)$_3$}, \tag{3}$$

resulting in significant changes of the structural specification present. As the temperature increases, the right side of the equilibrium is increasingly favored. From the temperature dependence of the equilibrium constant, a reaction enthalpy value near 50 kJ/mol was obtained.\(^{25}\)

**TABLE II.** Parameters $y$ and $z$ for possible and hypothetical molecular units in the $\text{P-Se}$ system. Hypothetical molecular units whose identity has not been experimentally documented are marked by asterisks.

<table>
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<tr>
<th>Compound</th>
<th>$y$</th>
<th>$z$</th>
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<tbody>
<tr>
<td>$\text{P$_5$Se$_5$}$</td>
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<td>0.75</td>
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<tr>
<td>$\text{P$_5$Se$_5$(M-V)$^*$}$</td>
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<td>0.5</td>
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<td>$\text{P$_5$Se$_5$}$</td>
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<td>0.5</td>
</tr>
<tr>
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<td>$\text{P$_4$Se$_7$}$</td>
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<tr>
<td>$\text{P$_5$Se$_5$}$</td>
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</table>

C. Comparison of present structure results with neutron diffraction and EXAFS results

It is instructive to compare glass structure results from the present NMR and Raman results with previous results based on a combined interpretation of neutron diffraction (ND) and extended x-ray-absorption fine-structure (EXAFS) experiments.\(^{7,8}\) In these previous studies, Price and co-workers have described the structure of the present glasses in terms of two parameters $y$ and $z$, where $y$ denotes the fraction of four-fold-coordinated $P$ atoms and $z$ the ratio of the number of $P$-P bonds to the number of $P$ atoms present. They have described their findings with reference to the molecular units $\text{P$_4$Se$_5$}$, $\text{P$_4$Se$_4$}$ (of which they use the particular isomer proposed by Monteil and Vincent\(^{16}\) and $\text{P$_5$Se$_5$}$, the structure of which was reported by Penney and Sheldrick.\(^{26}\) Table II summarizes the parameters $y$ and $z$ represented by these structures. We have further included the $y$ and $z$ parameters for $\alpha$- and $\beta$-$\text{P$_4$Se$_4$}$ (Fig. 1), for the molecular structure of $\text{P$_5$Se$_5$}$ of Blachnik et al., as well as for two hypothetical structures $\text{P$_5$Se$_7$} (x = 0.36)$ and $\text{P$_5$Se$_{10}$} (x = 0.29)$.

The comparison of these data illustrates that the speciation derived from NMR and Raman spectroscopies are in good agreement with each other, whereas they deviate substantially from those extracted from the previous ND-EXAFS results. At $P$ content $>30$ at.\%, ND and EXAFS indicate a substantially higher fraction of four-fold-coordinated $P$ atoms than found in NMR or Raman studies. Furthermore, the number of $P$-P contacts inferred from the ND-EXAFS results also exceeds that deduced from the present Raman and NMR results at all $x$. Finally, comparison of Tables II and III illustrates that the values of $y$ and $z$ observed as a function of $P$ content are by largemuch more consistent with the values observed for the various known molecular and crystalline structures in the $\text{P-Se}$ system. Contrary to Refs. 7 and 8, we do not observe $z$ to increase as a function of $P$ content in the glasses relative to the crystals. The present results do not support a model of $\text{P$_4$Se$_5$}$ clusters embedded in a selenium-rich matrix as a possible description of the present glasses.\(^{7,8}\)

D. Agglomeration theory, slope equations, and $T_g(x)$ variation

The agglomeration theory introduced by Kerner and Micoulaut\(^{15}\) provides a means to predict $T_g(x)$ trends when
agglomeration of atoms or molecules to form a glass network proceeds in a stochastic fashion. It is instructive to inquire what message is contained in the observed $T_g(x)$ trend of Fig. 2(a) given the local structural units established from the two spectroscopic probes. To address the issue, we outline the agglomeration theory as it relates to present binary glass system.

The central idea of the theory is to relate an increase of viscosity in a glass-forming liquid with creation of bonds between well-defined local structural configurations (LSC’s) at random. In the present case, we will consider two LSC’s consisting of two-fold-coordinated Se atoms (A) and five-fold-coordinated P atoms (B) as shown in Fig. 12.

Let us consider the statistics of bonding between LSC’s in a particular region of a liquid ($T>T_g$) at time $t=0$. Let us denote by $p_A(0)$ (the 0 in the parentheses refers to $t=0$) and $p_B(0)=1-p_A(0)$ the probability distributions for A and B LSC’s in the liquid. After a finite step $\tau_0$, these probabilities evolve and acquire new values $p_A(\tau_0)$ and $p_B(\tau_0)$ as bonds reform and LSC’s diffuse. Let $p_{AA}$ and $p_{AB}$ designate, respectively, the probabilities for atom A to bond with A and for atom A to bond with B. These probabilities depend on the coordination numbers of atoms A and B, the initial probabilities $p_A(0)$ and $p_B(0)$, and Boltzmann factors which involve bond energies and temperatures. Thus $p_A(\tau_0)$ can be written as

$$p_A(\tau_0) = \frac{1}{2} [p_{AA} + p_{AB}] - p_A(0),$$

At $T_g$, structural arrest manifests and fluctuations in the probabilities $p_A(\tau_0)-p_A(0)$ must vanish because LSC’s cease to move and are trapped. This condition serves to define $T_g$, as we will see later. In the present binary glass system, at low P content, there are three ways to connect P with Se (we exclude the possibility of P-P bonds): Se-Se, P-Se, and P=Se (Fig. 12). The probabilities $p_{Se-Se}$, $p_3$, and $p_4$ (Fig. 12) of these bonding configurations are given by

$$p_{Se-Se}(T) = \frac{4}{Z} (1-x)^2 e^{-\beta E_{Se-Se}},$$

$$p_3(T) = \frac{12}{Z} x(1-x) e^{-\beta E_{P-Se}},$$

$$p_4(T) = \frac{40}{Z} x(1-x) e^{-\beta E_{P=Se}},$$

where $Z$ represents the Partition function and $\beta = 1/k_B T$.

The Boltzmann factors appearing in Eqs. (5)–(7) take into account bond energies $E_{P-Se}$, $E_{P=Se}$, and $E_{Se-Se}$, while the statistical factors (12, 40, and 4) represent, respectively, the number of equivalent ways to connect a P atom to a Se atom to form single bonds [and create a P(Se$_{1/2}$3 structural unit] or to form double bonds [and create a Se=P(Se$_{1/2}$3 structural unit], or a Se atom to bond to another Se atom (to form part of a Se chain). These statistical factors can be regarded as degeneracies of corresponding energy states of a canonical system (here the different possible bond energies of the network). For simplicity, we will set $E_{P=Se}=E_{P-Se}+\Delta$ in the forthcoming. An equivalent way to think is to say that the probability $p_{Se}$ of Se atoms computed from a random distribution of bonds is only equal to the concentration $(1-x)$ of Se, when the entire network becomes connected at $T_g$. For $T>T_g$, we have $p_{Se} < 1-x$. At $T=T_g$, we have

$$p_{Se} = \frac{1}{2} [2p_{Se-Se} + p_3 + p_4] = 1-x,$$

which gives the same result as $p_A(\tau_0) = p_A(0)$. Equation (8) can be solved exactly from the aforementioned construction and yields

<table>
<thead>
<tr>
<th>$x$</th>
<th>$y$ (NMR)</th>
<th>$y$ (Raman)</th>
<th>$y$ (Refs. 7, and 8)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.05</td>
<td>0.43</td>
<td>n.d.</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.10</td>
<td>0.37</td>
<td>0.45</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.15</td>
<td>0.31</td>
<td>0.4</td>
<td>0.5–0.6</td>
</tr>
<tr>
<td>0.20</td>
<td>0.26</td>
<td>0.2</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.25</td>
<td>0.22</td>
<td>n.d.</td>
<td>0.25</td>
</tr>
<tr>
<td>0.30</td>
<td>0.15</td>
<td>0.15</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.35</td>
<td>0.11</td>
<td>0.08</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.40</td>
<td>0.05</td>
<td>0.05</td>
<td>0.25</td>
</tr>
<tr>
<td>0.45</td>
<td>0.01</td>
<td>n.d.</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.50</td>
<td>0</td>
<td>0</td>
<td>0.25(0.2)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>$x$</th>
<th>$z$ (NMR)</th>
<th>$z$ (Raman)</th>
<th>$z$ (Refs. 7, and 8)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.05</td>
<td>0</td>
<td>n.d.</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.10</td>
<td>0</td>
<td>0</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.15</td>
<td>0</td>
<td>0</td>
<td>0–0.4</td>
</tr>
<tr>
<td>0.20</td>
<td>0</td>
<td>0.25</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.25</td>
<td>0.05</td>
<td>n.d.</td>
<td>0.5</td>
</tr>
<tr>
<td>0.30</td>
<td>0.12</td>
<td>0.31</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.35</td>
<td>0.23</td>
<td>0.38</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.40</td>
<td>0.42</td>
<td>0.50</td>
<td>0.75</td>
</tr>
<tr>
<td>0.45</td>
<td>0.53</td>
<td>n.d.</td>
<td>n.d.</td>
</tr>
<tr>
<td>0.50</td>
<td>0.57</td>
<td>0.55</td>
<td>1.10 (0.9)</td>
</tr>
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</table>
where \( e_{P,Se} = \exp[-(E_{P,Se} - E_{Se,Se})/k_B T_g] \) and \( e_{P-Se} = \exp[-(E_{P-Se} - E_{Se,Se})/k_B T_g] \). One can reduce the number of parameters appearing in Eq. (9) by considering the \( x \to 0 \) limit, with the glass transition temperature \( T_g \to T_0 \), the glass transition temperature of Se glass. From Eq. (9), we obtain

\[
E_{P,Se} - E_{Se,Se} = k_B T_0 \ln \left[ \frac{3 + 10e^{\Delta(r_0)}}{2} \right].
\]

Equation (10) then becomes, in the limit \( T_g \to T_0 \)

\[
E_{P,Se} - E_{Se,Se} = k_B T_0 \ln \left[ \frac{3}{2(1 - \eta)} \right].
\]

In Eq. (12), the condition \( \eta = 1 \) is to be excluded, because it implies an infinite value for the energy difference \( \Delta = E_{P,Se} - E_{P,Se} \), thus leading to a network composed of \( P=Se \) links only, which is clearly unphysical. With the energy differences established, Eq. (9) provides a relation between \( T_g \) and \( x \) with only one parameter, the fraction of fourfold-coordinated \( P \) units in the glasses.

Finally, the relationship (9) can be cast in a more compact form: if the slope at \( x \to 0 \), the origin is computed. Upon the insertion of the established energy difference from Eq. (12), one obtains the final slope equation result:

\[
\frac{dT_g}{dx} \Bigg|_{x=0} = \frac{3}{T_0 \ln(2(1 - \eta))}.
\]

At low \( x \), two types of \( P \)-cation sites occur and we find that the slope \( (dT_g/dx) \) at the origin depends on the parameter \( \eta \), the fraction of fourfold-coordinated \( P \) units. In other chalcogenide systems such as the \( Ge_xX_{1-x} \) \( (X=Se,Te) \), wherein only one cation site is formed, the slope \( dT_g/dx \) actually becomes parameter free\(^{28}\) and equals \( T_0/\ln(r_{Ge}/r_{Se}) = T_0/\ln 2 \), in excellent agreement with experiments.

Equation (13) reveals that when \( \eta = 0 \) the slope \( dT_g/dx \) equals to \( T_0/\ln 1.5 \). The slope decreases to \( T_0/\ln 3 \) at \( \eta = 1/2 \), however. The latter result is not obvious. It is, for example, difficult to see how the connectivity of a network would change by the inclusion of a finite fraction of fourfold-coordinated \( P \) atoms (\( \eta \neq 0 \)) in the backbone when these only provide three linkages to the rest of the network, as do the threefold-coordinated \( P \) atoms in \( P(Se_{1/2})_3 \) units. The answer resides in the recognition that the presence of fourfold-coordinated \( P \) atoms in addition to the threefold-coordinated \( P \) atoms drastically increases the total number of ways in which \( P \) and \( Se \) atoms can bond to each other to produce possible clusters. The denominator in the slope, Eq. (13), is related to the entropy of the network. Thus an increase in connectivity of a network can also result from an increase in the number of accessible structural states accounting for a decrease in the slope \( dT_g/dx \) at finite \( x \).

\(^{31}P \) NMR measurements\(^{11}\) reveal that \( \eta \), starting from a value of 1/2 at \( x \to 0 \), extrapolates almost linearly to zero as \( x \) increases to 0.45. Taking such a variation of \( \eta(x) \) into account, we have calculated the expected \( T_g(x) \) variation [Eq. (13)] given by the stochastic agglomeration theory. The result is projected in Fig. 2(a) as the dashed line. One finds that the agreement between theory and experiment is excellent at \( x \leq 0.12 \), but at higher \( x \), a systematic deviation sets in. Our interpretation of these results is that in the \( 0 < x < 0.12 \) composition range, the present glasses can be visualized as a stochastic network composed of \( Se \) chain fragments bridging pyramidal \( P(Se_{1/2})_3 \) and quasitetrahedral \( Se=P(Se_{1/2})_3 \) units in a random fashion. At higher \( x \), new building blocks composed of ethylenelike \( P_3(Se_{1/2})_4 \) polymeric units emerge and further reduce the slope \( dT_g/dx \) (0.15 < \( x < 0.45 \)) by increasing the possible number of pathways in which these three different types of \( P \)-centered local units can agglomerate.

Stochastic theory suggests that the increase in the number of pathways to agglomerate lowers the slope, \( dT_g/dx \) at \( x > 0.12 \). At \( x > 0.45 \), only two building blocks contribute to the network backbone, \( Se_{1/2} \)-chain fragments and \( P_3(Se_{1/2})_4 \) units, and one finds that the slope \( dT_g/dx \) increases drastically as the number of pathways in which clusters can form is severely reduced.

IV. CONCLUDING REMARKS

The rich Raman scattering and \(^{31}P \) NMR line shapes on melt-quenched \( P_xSe_{1-x} \) glasses have been decoded to yield the concentrations of \( Se_{1/2} \)-chain, pyramidal \( P(Se_{1/2})_3 \), quasitetrahedral \( Se=P(Se_{1/2})_3 \), polymeric \( P_3(Se_{1/2})_4 \), and monomeric \( P_4Se_3 \) units at \( x < 0.50 \). Such information has provided a means to decode the global connectivity of the backbone and to quantitatively account for the observed \( T_g \) variation with \( x \) at low \( x \) using stochastic agglomeration theory.

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