

MATLAB

Suppose you have a set of nodal equations, such as Practice Problem 4.1 on page 83 of the text:

$$\begin{aligned} 4v_1 - v_2 &= -75 \\ -4v_1 + 19v_2 &= 120 \end{aligned}$$

You can use Cramer's rule and solve 2x2 determinants to find $v_1 = -18.125$ V and $v_2 = 2.5000$ V.

You can also solve this with MATLAB. We have $A*V = C$, where

$$\begin{array}{ccc} A = \begin{bmatrix} 4 & -1 \\ -4 & 19 \end{bmatrix} & V = \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} & C = \begin{bmatrix} -75 \\ 120 \end{bmatrix} \end{array}$$

Solving the system simultaneously simply means finding $V = A^{-1} * C$, where A^{-1} is the inverse of A , i.e., $A^{-1} * A = 1$.

Open MATLAB and you will see something like the following:

< M A T L A B >

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To get started, select MATLAB Help or Demos from the Help menu.

Type in the coefficients, $A = [4 \ -1; -4 \ 19]$, and hit "return" (be sure to put a space after 4 and -4); MATLAB will print the following:

```
A =  
 4  -1 ← row 1  
-4  19 ← row 2
```

Now type in the right-hand side, $C = [-75; 120]$, and hit "return"; MATLAB will print the following:

```
C =  
-75  
120
```

Now type in $V = A^{-1} * C$ and hit "return"; MATLAB will print the following:

```
V =  
-18.1250  
 2.5000
```

Compare with Practice Problem 4.1 in the text.

MATLAB can save a lot of labor with large determinants, that is, more nodes.

Consider Example 4.2 on pages 83-84; the three nodal equations are:

$$0.5833 v_1 - 0.3333 v_2 - 0.2500 v_3 = -11$$

$$-0.3333 v_1 + 1.4762 v_2 - 0.1429 v_3 = 3$$

$$-0.2500 v_1 - 0.1429 v_2 + 0.5929 v_3 = 25$$

The text example uses Cramer's rule, which requires you to solve 3x3 determinants. The MATLAB solution is:

```
>> A=[0.5833 -0.3333 -0.2500;-0.3333 1.4762 -0.1429;-0.2500 -0.1429 0.5929]
```

```
A =
```

```
    0.5833   -0.3333   -0.2500  
   -0.3333    1.4762   -0.1429  
   -0.2500   -0.1429    0.5929
```

```
>> C=[-11;3;25]
```

```
C =
```

```
   -11  
     3  
    25
```

```
>> V=A^-1*C
```

```
V =
```

```
    5.4124  
    7.7375  
   46.3127
```

```
>>
```

Compare with the values on page 84 of the text found using Cramer's rule.

Using MATLAB (see appendix 2)

$$\begin{bmatrix} 0.5833 & -0.3333 & -0.25 \\ -0.3333 & 1.4762 & -0.1429 \\ -0.25 & -0.1429 & 0.5929 \end{bmatrix} \begin{bmatrix} \sqrt{1} \\ \sqrt{2} \\ \sqrt{3} \end{bmatrix} = \begin{bmatrix} -11 \\ 3 \\ 25 \end{bmatrix}$$

3x3 matrix a

column vector b

column vector c

$$a b = c$$

$$\text{solution } b = a^{-1} c$$

In MATLAB, we write

$$\gg a = \begin{bmatrix} 0.5833 & -0.3333 & -0.25 \\ -0.3333 & 1.4762 & -0.1429 \\ -0.25 & -0.1429 & 0.5929 \end{bmatrix};$$

$$\gg c = [-11; 3; 25];$$

$$\gg b = a^{-1} * c$$

$$b = \begin{bmatrix} 5.4124 \\ 7.7375 \\ 46.3127 \end{bmatrix}$$

← solution returned by MATLAB

>>

Solving KCL using the symbolic processor on MATLAB.

$$\gg \text{eqn1} = '-8-3 = (V_1 - V_2)/3 + (V_1 - V_3)/4 \quad | \quad ;$$

$$\gg \text{eqn2} = '-(-3) = (V_2 - V_1)/3 + V_2/1 + (V_2 - V_3)/7 \quad | \quad ;$$

$$\gg \text{eqn3} = '-(-25) = V_3/5 + (V_3 - V_2)/7 + (V_3 - V_1)/4 \quad | \quad ;$$

$$\gg \text{answer} = \text{solve}(\text{eqn1}, \text{eqn2}, \text{eqn3}, 'V_1', 'V_2', 'V_3');$$

$$\gg \text{answer.V1}$$

$$\text{ans} =$$

$$720/133$$

solution is returned as a 'structure'

$$\gg \text{answer.V2}$$

$$\text{ans} =$$

$$147/19$$

$$\gg \text{answer.V3}$$

$$\text{ans} =$$

$$880/19$$

\gg