

Algorithms:

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1. a) Definitions: Connected Graph.
Connected Component
Spanning tree
MST
- b) Give an algorithm to find the #components in a graph.
Use algorithm to trace following adj matrix and show that #components in this example is 2.

$$A[G, J] = \begin{bmatrix} \text{- Given -} \end{bmatrix}$$
- c) Sample Graph Given. (15 nodes)
Find MST using Kruskal's Alg.
- d) What special data structures are used in Kruskal
Explain how they are used in Kruskal's alg.

2.

- a) Define: NP
Class Co-NP
Class NP-complete.
- b) State Cook's theorem.
- c) Show CNFSAT \propto CLIQUE.

Operating Systems:

1. $k = \# \text{ frames} = 4$.
Stream is : 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- a) Show page replacements, #faults, #hits in FIFO, LRU. Show data structures used.
- b) Give an algorithm OPT which will give minimum #faults provided the entire stream is known in advance.

c) What is Belady's anomaly?
 Show it for an algorithm for above referen stream.

d) Let $\{p_0, p_1, \dots, p_n\}$ be a page reference stream
 K - # frames in memory.

C_K - minimum constant

Show that:

$$\left[\begin{array}{c} \# \text{ faults for } \{p_0, \dots, p_n\} \\ \text{using FIFO} \end{array} \right] \geq C_K \times \left[\begin{array}{c} \# \text{ faults for } \{p_0, \dots, p_n\} \\ \text{using OPT} \end{array} \right] + b_0$$

Show that $C_K = K$. b_0 - constant.

2. 3 strategies :
- 1) No Preemption
 - 2) Preemption without timeslice
 - 3) Preemption, $t_s = 2ms$.

Job	Arrival	CPU(req)	Priority
1	0	4	1
2	1	3	2
3	2	2	3
4	2	3	2
5	3	4	1

Each process gets an I/O request every 1ms.

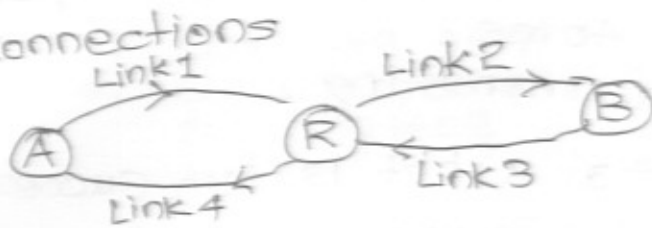
Each I/O request takes 2ms to complete.

Enough I/O devices so that processes need not compete for I/O device.

Find for each strategy,
 throughput, waiting time, turnaround time
 and compare.

WORKS:

CP Connections



→ Link 1 & 4 : 100 Mbps

Link 2 & 3 : 10 Mbps

→ A sends a very large file to B. Data travels via A to R to B in Link 1 & Link 2. ACK from B comes in Link 3 & Link 4.

→ Congestion Window size initially 16 Kb (??)

→ Data Segment size (including headers) = 1280 bytes

ACK size is 0.

→ Prop delay on each link = 10ms.

→ R has buffer of 10 packets and does tail drop queuing.

→ B has 1 packet buffer.

a) What is the min time between 2 ACK received at A.

b) What is the RTT.

c) If CW is quadrupled what will happen to throughput

d) If A is transmitting packet 15, where will other packets be? what is the state of R?

2.

a) Large # users use ALOHA with 50 requests/second.
Time is slotted at 40ms.
 p - probability of transmitting.

i) What is the prob. that a pkt is txn successfully?

ii) Wt is the prob. that k collisions occur and then packet is transmitted successfully?

iii) Wt is the avg # txn for successful txn?

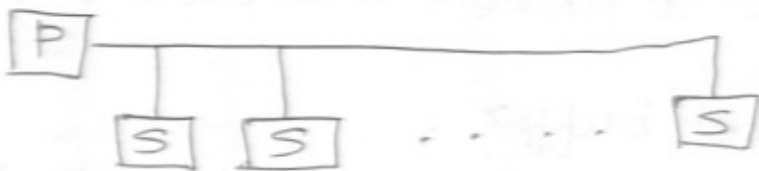
b) P - Primary

S - Secondary.

→ System uses roll call polling.

→ There are N secondaries.

→ $\alpha = \frac{\text{delay}_{\text{prop}}}{\text{delay}_{\text{txn}}}$. → $\text{delay}_{\text{prop}}$ is the prop. delay from P to last S.



(i) If only one S wants to transmit data (last S) show that
throughput $\approx \frac{1}{1+N\alpha}$

(i) If all S are ready to transmit data show that
throughput $\approx \frac{1}{1+\alpha}$