

The thermally reversing window in ternary $\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ glasses

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Abstract

$\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ glasses in the compositional range $0.05 \leq x \leq 0.19$ have been synthesized and examined in temperature modulated differential scanning calorimetry (MDSC) and Raman scattering experiments. Trends in the non-reversing enthalpy $\Delta H_{\text{nr}}(x)$ near T_g show the term to almost vanish in the $0.090(5) < x < 0.135(5)$ range, and to increase by an order of magnitude at $x < 0.09$, and at $x > 0.135$. In analogy to previous results on chalcogenide glasses, we identify compositions at $x < 0.09$ to be elastically *floppy*, those in the $0.090 < x < 0.135$ range to be in the *intermediate phase*, and those at $x > 0.135$ to be *stressed rigid*. MDSC results also show that the ΔH_{nr} term *ages* in the stressed-rigid and floppy phases but *not* in the intermediate phase. The intermediate phase is viewed to be a self-organized phase of a disordered network. It consists of at least four isostatically rigid local structures: corner-sharing GeS_4 , edge-sharing GeS_2 , pyramidal $\text{P}(\text{S}_{1/2})_3$ and quasi-tetrahedral $\text{S}=\text{P}(\text{S}_{1/2})_3$ units for which evidence comes from Raman scattering. The latter method also shows the existence of P_4S_7 and P_4S_{10} molecules in the glasses segregated from the backbone. These aspects of structure contribute to an intermediate phase that is significantly narrower in width than in the corresponding selenide glasses.

(Some figures in this article are in colour only in the electronic version)

1. Introduction

Under certain conditions disordered networks can self-organize. The recognition emerged [1] from the observation on binary $\text{Si}_x\text{Se}_{1-x}$ glasses of *two* elastic phase transitions as a function of network connectedness. In Raman scattering, the optical elasticity displays two thresholds: a second-order threshold near $x = x_c(1) = 0.20$ and a first-order one near $x = x_c(2) = 0.27$. In modulated differential scanning calorimetry (MDSC) measurements, the non-reversing enthalpy (ΔH_{nr}) near T_g displays an almost square-well-like behaviour with the walls located

near $x_c(1)$ and $x_c(2)$, and with the heat-flow term nearly vanishing in the well, $x_c(1) < x < x_c(2)$. Such thermally reversing windows that coincide with Raman optical elasticity thresholds have now been observed [2–5] in other chalcogenide glass systems, underscoring the generality of the observation.

A solitary elastic phase transition in random networks from an elastically floppy to stressed-rigid state was predicted by Phillips [6] and Thorpe [7] in the early 1980s. An important step in understanding the origin of two elastic phase transitions came from the numerical simulations of Thorpe *et al* [8] who suggested that the first transition represents the onset of rigidity ($x_c(1)$) and the second transition the onset of stress ($x_c(2)$) in the backbone of these glasses. The intervening region, the intermediate phase, represents then a rigid but stress-free domain of a disordered network identified with the *self-organized* phase of a glass. Micoulaut and Phillips [9] have more recently introduced an analytical method called size increasing cluster agglomeration (SICA) to estimate the compositional range of the intermediate phase in Si–Se glasses. The method starts from the appropriate local structures, and these are then agglomerated in steps to build medium range structures. Constraint counting algorithms [9] then permit establishing the chemical compositions where rigidity onsets $x_c(1)$, and then stress onsets $x_c(2)$ in these clusters as they are cross-linked progressively. The intermediate phase estimated by SICA is in good agreement with the experimental results on Si–Se and Ge–Se glasses. SICA calculations become progressively more intensive as the number of local structures and agglomeration steps are increased.

In this work we examine the nature of elastic phases in ternary $\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ glasses. The glass structure is studied using Raman scattering, and the thermal properties of the glasses including T_g are examined in MDSC measurements. These results permit a detailed comparison of the intermediate phase in the present glasses with that in the corresponding selenides [5]. The comparison provides new insights into aspects of molecular structure that control the width of the self-organized phase when Se is replaced by S. Self-organization effects in disordered systems represent a recent and exciting issue in glass science that has profound consequences in a number of fields including protein folding [10], thin-film gate dielectrics [11] for CMOS devices, and the origin of high-temperature superconductivity [12]. The subject is close to the continuing interests [13] of Thorpe, and it is, indeed, a pleasure to dedicate this contribution to celebrate his 60th anniversary.

2. Experimental details

2.1. Sample synthesis

99.999% elemental Ge, S and P, from Cerac Inc., were used as starting materials to synthesize ternary $\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ glasses in the compositional range $0.05 \leq x \leq 0.19$. One gram batches were sealed in evacuated (5×10^{-7} Torr) quartz ampoules and slowly (2 days) heated to 950 °C. Melts were homogenized for 3 days in a rocking furnace. They were then equilibrated at 30–50 °C above the liquidus for 6 h before a water quench to obtain the glasses. At low x (<3%) and high x (>24%), we were unable to obtain uniform glasses. Once synthesized, the samples were handled in a dry nitrogen ambient and stored in evacuated Pyrex tubings.

2.2. MDSC results

A model 2920 MDSC from TA instruments Inc., operated at 3 °C min⁻¹ scan rate and 1 °C/100 s modulation rate, was used to examine the glass transitions [14]. Samples aged at room temperature for 2 weeks or longer were scanned up in temperature past T_g and then cooled back to room temperature. T_g was deduced from the inflexion point of the reversing heat

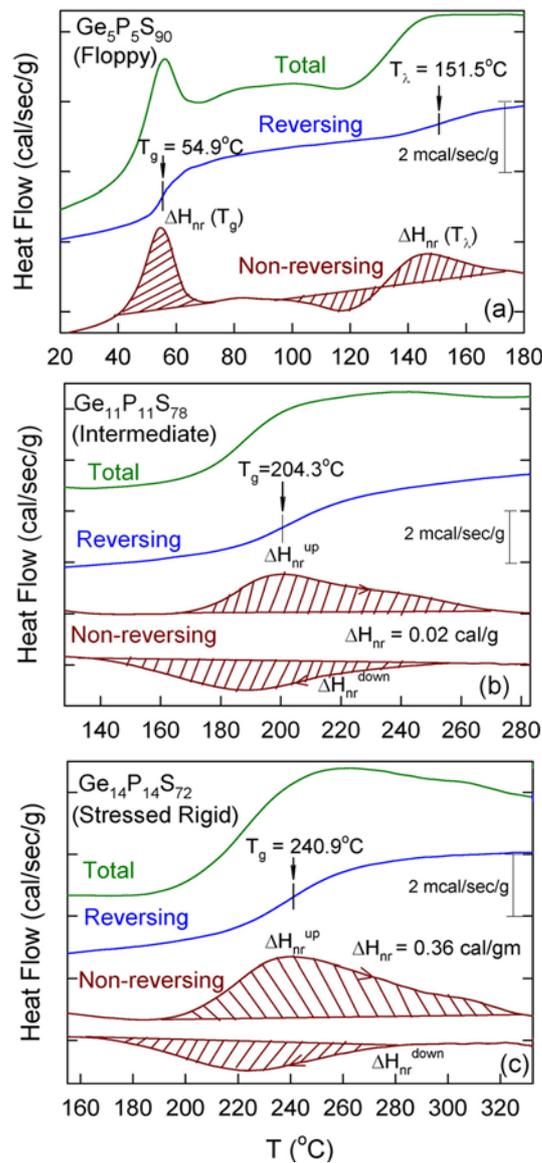


Figure 1. MDSC scans of $\text{Ge}_x\text{P}_x\text{S}_{100-2x}$ glasses at: (a) $x = 5$, floppy glass; (b) $x = 11$, intermediate phase glass; and (c) $x = 14$, stressed rigid glass; each taken at $3^{\circ}\text{C min}^{-1}$ scan rate, $1^{\circ}\text{C}/100 \text{ s}$ modulation rate. The total (green), reversing (blue) and non-reversing (red) heat flow terms are shown. The later scanning up in T (right arrow) and then down (left arrow) are illustrated in (b) and (c). The frequency corrected $\Delta H_{nr} = \Delta H_{nr}^{up} - \Delta H_{nr}^{down}$ nearly vanishes for a glass at $x = 11$ shown in (b). See the text for details.

flow signal. At $x = 0.05$, one observes, in general, two endotherms in the glasses (figure 1(a)): one near 55°C and the other near 150°C . Here, the low- T endotherm represents the glass transition temperature while the high- T endotherm represents the polymerization [15, 16] transition T_λ of sulfur. With increasing x , the low- T endotherm moves up in T while the high- T endotherm remains nearly fixed near $T = 150^{\circ}\text{C}$.

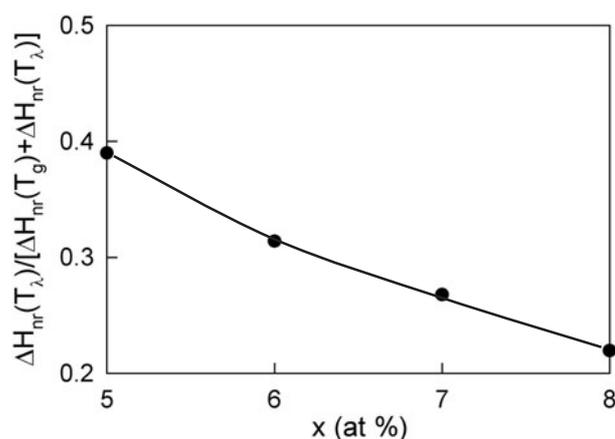


Figure 2. Normalized non-reversing term associated with the T_λ endotherm, $\Delta H_{nr}(T_\lambda)$, showing a steadily decreasing value with x in the range $5\% < x < 8\%$. The data reveal a two-fold reduction in S_8 concentration across the indicated range of x .

A characteristic feature of the T_λ transition is the unusual non-reversing heat flow associated with it: an exotherm followed by an endotherm. It appears that S_8 crowns relax towards the backbone (exotherm) prior to opening into S_n -chain fragments (endotherm). In orthorhombic S , where there is no network backbone, the T_λ transition [16] consists of an endotherm alone. In the present glasses the normalized integrated area under the T_λ -endotherm decreases with x , and it reflects the concentration of the S_8 crowns decreasing and eventually vanishing near $x = 0.09$ (figure 2).

The non-reversing heat flow extracted from the difference of the *total*- and *reversing*-heat flow signals scanning up in temperature suffers from an overestimate due to an upshift of the latter signal because of the finite scan rate employed (3°C min^{-1}). To correct [17] for this shift, one scans down in temperature across T_g after scanning up. One then obtains the corrected ΔH_{nr} term by taking the difference between the non-reversing heat flow scanning up in T ($\Delta H_{nr}^{\text{up}}$) from the non-reversing heat flow coming down in T ($\Delta H_{nr}^{\text{down}}$) as shown in figure 1(b). In the latter scan, the reversing heat flow signal downshifts in T as much as it upshifts in the scan up in T . Henceforth, the corrected non-reversing heat flow term will simply be referred as ΔH_{nr} . For the glass composition at $x = 0.11$, one can see from figure 1(b) that the ΔH_{nr} term of 0.02 cal g^{-1} is minuscule.

Figure 3(a) gives a summary of the compositional variation in $T_g(x)$ of the glasses. We find $T_g(x)$ to increase monotonically with x , at first sharply in the $0.05 < x < 0.10$ range and thereafter more slowly once $x > 0.10$. Figure 3(a) also shows glass compositions across which the T_λ transition is observed. Compositional trends in $\Delta H_{nr}(x)$ are summarized in figure 3(b), in which we display results on glass samples aged for 2 weeks after melt-quenching, and separately for 8 weeks. The results of figure 3(a) bring out the exceptional behaviour of glass compositions in the $0.09 < x < 0.135$ range; these glasses possess a vanishing ΔH_{nr} term and that term does not age. On the other hand, glass compositions at $x < 0.09$ and at $x > 0.135$ not only possess an order of magnitude larger ΔH_{nr} term but that term also appears to age noticeably.

2.3. Raman scattering

Raman scattering was excited using 1 mW of 514.5 nm radiation loosely focused to a $50 \mu\text{m}$ laser spot size on glass samples encapsulated in quartz tubings, which were used to synthesize

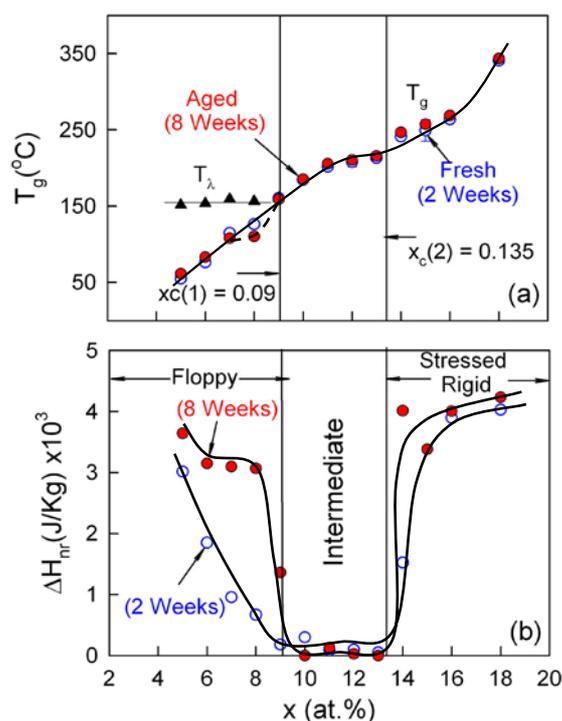


Figure 3. MDSC results on present glasses showing trends in (a) $T_g(x)$ and (b) $\Delta H_{nr}(x)$ as a function of x and ageing. Filled triangles give the T_λ transition observed in S-rich glasses. A sharply defined square-well-like thermally reversing window is observed in the 8 week aged samples in (b) while the T_g s vary monotonically across this window in (a).

the samples. The back-scattered radiation was analysed using a model T-64000 triple-monochromator system [4, 16] from Jobin Yvon Inc., using a charge coupled device detector. Figure 4(a) gives an overview of the observed Raman line shapes at several glass compositions. At low x (5%–9%), the line shapes are dominated by modes [15, 16] of elemental S at 150, 215 and 485 cm^{-1} that steadily decrease in scattering strength as x increases. Concomitantly, one observes an increase in scattering strength of several modes: corner-sharing (CS) GeS_4 tetrahedra at 345 cm^{-1} , edge-sharing (ES) $\text{Ge}(\text{S}_{1/2})_4$ tetrahedra at 375 cm^{-1} , pyramidal (PYR) $\text{P}(\text{S}_{1/2})_3$ units at 416 cm^{-1} and quasi-tetrahedral (QT) $\text{S}=\text{P}(\text{S}_{1/2})_3$ tetrahedra near 700 cm^{-1} and 375 cm^{-1} . At higher x , sharp modes of P_4S_{10} and P_4S_7 monomers appear in the line shape. In the spectra, we can also observe sharp modes of the P_4S_4 and P_4S_3 monomers (containing P–P bonds) at $x > 0.15$ highlighted in the inset of figure 4(a). An enlarged view of the two insets of figure 4(a) appears as figures (b) and (c) in which the mode assignments of the different species are indicated.

Table 1 gives a summary of the vibrational mode assignments in the present glasses. These assignments were made feasible by earlier vibrational studies on binary Ge–S glasses [18, 19], P–S glasses [20–22], crystalline molecular solids [23–25] in the P–S binary, and amorphous P [26–28], as well as first-principles cluster calculations [29, 30]. Figure 5 provides a schematic drawing of these local structures, some of which form part of the backbone while others segregate as molecules in the glasses. We shall return to discuss these results in section 3.

The observed line shapes were least-squares fitted to the requisite number of Gaussians with unrestricted line-width, centroid and intensity. An example is shown in figure 4(d), that

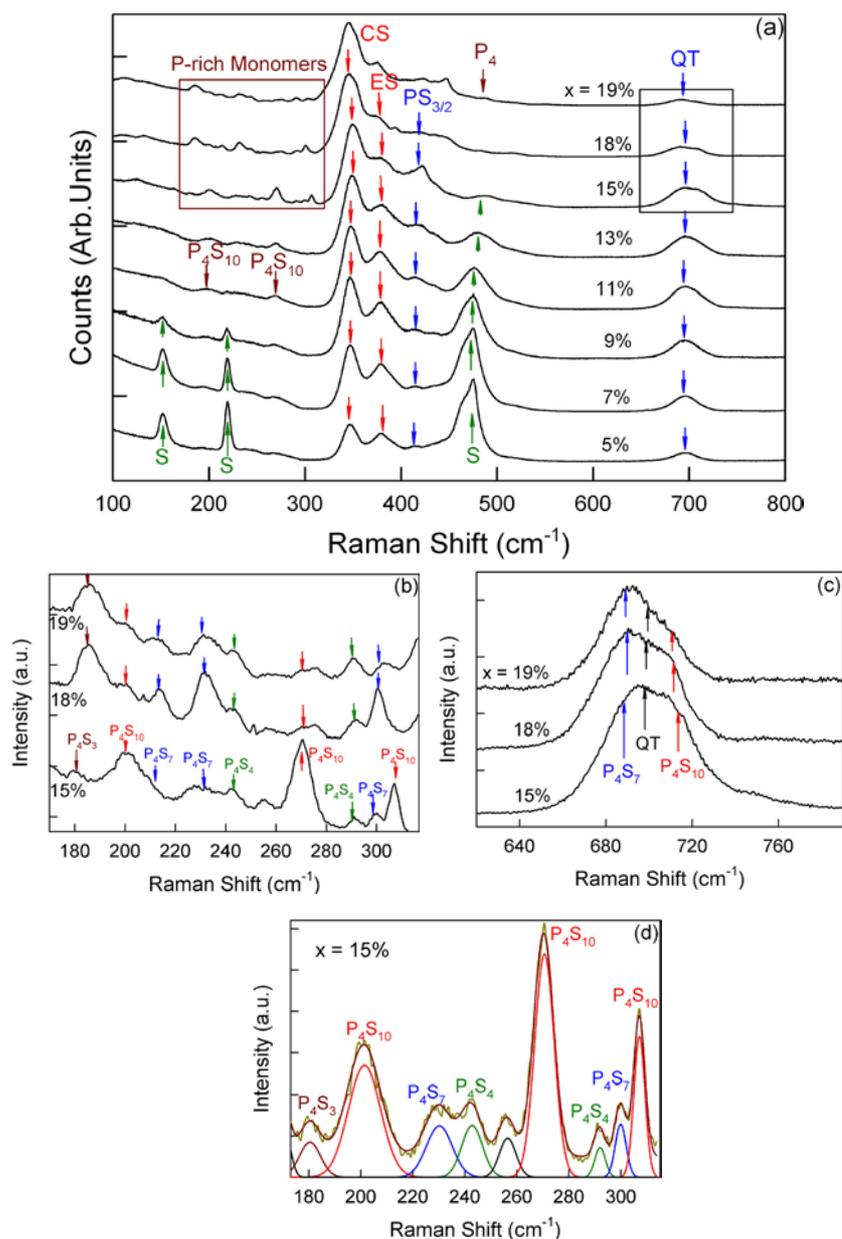


Figure 4. (a) Observed Raman scattering lineshapes as a function of x with principal modes labelled. (b) and (c) give a blow-up of the insets shown in (a). Sharp modes of P-rich monomers P_4S_3 , P_4S_4 , P_4S_7 and P_4S_{10} and QT units are labelled in (b) and (c). (d) An example of a deconvolution of a Raman lineshape at $x = 15\%$.

provides line shape analysis of the low-frequency segment of a glass sample at $x = 0.15$. One can clearly identify the vibrational modes of characteristic monomers (table 1). In our analysis of these line shapes we have used a software package, Peak-Fit, marketed by SPSS Inc., to deconvolute the line shapes. The normalized scattering strength of the 700 cm^{-1} mode (QT

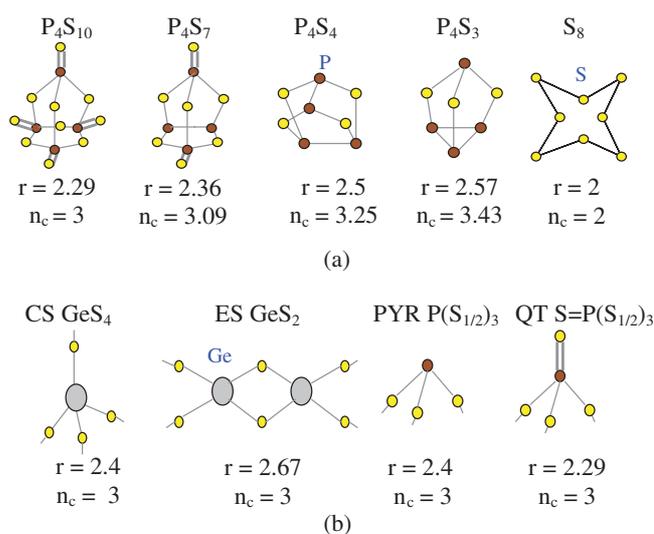


Figure 5. Ball and stick diagrams of (a) monomeric molecular units and (b) isostatic network forming units observed in the present ternary glasses. The mean co-ordination number \bar{r} and the count of constraints per atom (n_c) are also shown. See also table 2.

Table 1. Summary of vibrational mode assignments of various molecular units present in the titled glasses.

Mode frequency (cm^{-1})	Mode labels	Local structures	References
150, 218, 475	S_n	S-chains and Rings	[18]
185, 286, 342, 421, 441, 488	$P_4S_3^m$	P_4S_3	[24]
189, 217, 232, 303, 346, 444	$P_4S_7^m$	P_4S_7	[25]
196, 270, 715	$P_4S_{10}^m$	P_4S_{10}	[26]
243, 285, 440, 462	$P_4S_4^m$	P_4S_4	[55]
346	CS	Corner sharing GeS_4	[29, 4]
375	ES	Edge sharing GeS_2	
389, 398, 425, 458, 500	a-P	Amorphous P	[27]
416	PYR	$P(S_{1/2})_3$	[20]
440	F_2	Face sharing $\text{GeS}_{4/2}$	[4]
465, 606	P_4	P_4 clusters	[28]
700, 375	QT	$S=P(S_{1/2})_3$	[20, 22]

units), 345 cm^{-1} mode (CS units), 270 cm^{-1} mode (P_4S_{10} units), 185 cm^{-1} mode (P_4S_3 units), 230 cm^{-1} mode (P_4S_7 units) are summarized in figure 6. On this plot the scattering strength of the indicated modes were normalized to the total area. No attempts to obtain Raman cross sections of the mode were made. Until these matrix element effects are folded in, Raman scattering strengths can serve only as a qualitative guide of local structure concentrations.

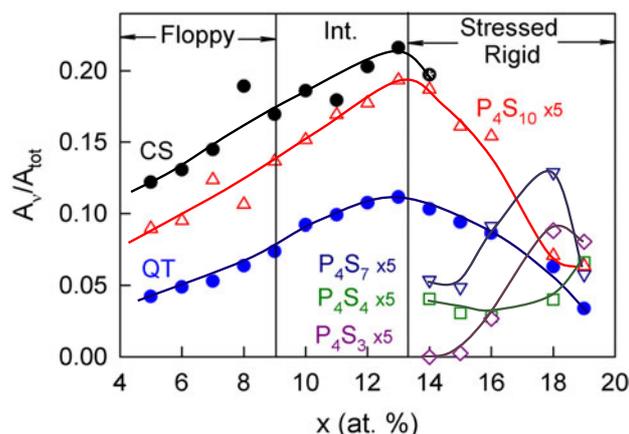


Figure 6. Raman scattering strengths of various vibrational modes of specific molecular units in ternary Ge-P-S glasses plotted as a function of x . The CS mode strength could not be reliably ascertained at $x > 13\%$ because of overlap with modes of other units. Note that the scattering strength of modes of the monomers, P_4S_{10} , P_4S_4 , P_4S_7 and P_4S_3 are scaled up by a factor of 5 to display on the same y-axis scale.

Table 2. Chemical bond strengths of several heteropolar and homopolar bonds among Ge, P, S and Se taken from [32].

Bond type	Pauling single bond strength (kcal mol ⁻¹)
P-P	51.3
Ge-Ge	37.6
S-S	50.9
P-S	54.8
P-Se	51.72
Ge-S	55.52
Ge-Se	49.08

3. Discussion

3.1. Evolution of glass structure with chemical composition

3.1.1. Low cation concentration x (< 0.10). Sulfur melts upon cooling form molecular crystals [16] composed of S_8 crowns. The behaviour is unlike that of selenium melts that give rise to a glass composed of polymeric Se_n -chain fragments upon cooling. There have been efforts to rapidly quench sulfur melts to form bulk glasses, and a T_g of about 255 K or -18°C has been reported [31]. The low T_g is suggestive of a zero-dimensional glass composed largely of S_8 monomers coupled by weaker van der Waals forces. In general, it is difficult to form homogeneous S-rich bulk glasses with trace amounts of group IV and V additives largely because of the tendency of S_8 crowns to segregate in such samples. At room temperature, these monomers are chemically more stable than S_n -chains.

On chemical grounds one may expect P and Ge additives in a sulfur melt to result in the formation of heteropolar bonds because the respective single P-S ($54.8 \text{ kcal mol}^{-1}$) and Ge-S ($55.5 \text{ kcal mol}^{-1}$) bond strengths [32] (table 2) exceed the homopolar bond strengths of S-S ($50.9 \text{ kcal mol}^{-1}$), Ge-Ge ($37.6 \text{ kcal mol}^{-1}$) and P-P ($51.3 \text{ kcal mol}^{-1}$). Specific P-

centred and Ge-centred local structures consistent with the chemical valence of P and Ge can be expected to form in the present ternary glasses as they do in the corresponding binary (Ge–S, P–S) glasses [18–22]. The prevailing P-centred and Ge-centred local structures populated in the present glasses include PYR [$\text{P}(\text{S}_{1/2})_3$], QT [$\text{S}=\text{P}(\text{S}_{1/2})_3$], CS [GeS_4] and ES [GeS_2] for which Raman vibrational evidence is available from our results (figure 4 and table 1).

The molecular structure of S-rich glasses is thus expected to be intrinsically heterogeneous and to consist of S_8 crowns and a network backbone composed of specific P- and Ge-based local structures serving to cross-link S_n -chains. With increasing cation concentration x , one expects the network backbone to grow at the expense of the S_8 monomer fraction. The former structural grouping gives rise to a glass transition temperature, T_g , while the latter monomers give rise to the T_λ transition as observed in our MDSC scans (figure 1(a)). Our experiments show that as x increases to 0.09, the S_8 monomer fraction becomes minuscule (figure 2).

3.1.2. High cation concentration $x (>0.10)$. At higher x ($10\% < x < 15\%$), more tetrahedral units (GeS_4), pyramidal units ($\text{P}(\text{S}_{1/2})_3$) and quasi-tetrahedral units ($\text{S}=\text{P}(\text{S}_{1/2})_3$) appear in the backbone as revealed by an increase in scattering strengths of their vibrational modes (figure 6). In addition to these network forming local structures, our Raman scattering results also reveal monomers of P_4S_{10} and P_4S_7 to systematically grow in concentration with increasing x (figures 4 and 6). The P_4S_{10} monomers first appear in the glasses at $x = 0.05$, and their concentration steadily increases to peak near $x = 0.13$. These units persist (figure 6) across the intermediate phase ($0.09 < x < 0.135$). The P_4S_{10} monomers convert to P_4S_7 ones, their P-richer counterparts, in the $0.15 < x < 0.19$ range as S is depleted from the glasses. The view is corroborated from the low-frequency (figure 4(b)) and high-frequency modes (figure 4(c)) of the P_4S_7 species that increase in strength with x .

In the present ternary glasses, one expects a chemical threshold [2] to occur when x increases to $x_t = 2/11$. If we require P to be three-fold and Ge to be four-fold coordinated to S, then on stoichiometric grounds one must require

$$\text{P}_x\text{Ge}_x\text{S}_{1-2x} = [\text{P}(\text{S}_{1/2})_3]_x[\text{Ge}(\text{S}_{1/2})_4]_x[\text{S}_{1-2x-7x/2}]. \quad (1)$$

A chemical threshold will appear when there is not enough S per P and Ge atom to permit pyramidal $\text{P}(\text{S}_{1/2})_3$ units and tetrahedral $\text{Ge}(\text{S}_{1/2})_4$ units to be formed in the network. The condition will occur when the free S content in equation (1) vanishes, i.e.,

$$1 - 2x_t - 7x_t/2 = 0, \quad \text{or} \quad x_t = 2/11. \quad (2)$$

Homopolar (Ge–Ge, P–P) bonds can be expected to emerge at $x > x_t$. However, since P–P bonds ($51.3 \text{ kcal mol}^{-1}$) are more strongly bound than Ge–Ge bonds ($37.6 \text{ kcal mol}^{-1}$, table 2), one expects P–P bonds to appear in the network at $x < x_t$, and thereby delaying the appearance of Ge–Ge bonds to a value of $x > x_t$. The appearance of the latter bonds in the glasses can be established using ^{119}Sn Mossbauer spectroscopy as recently demonstrated [2] in ternary $\text{Ge}_x\text{As}_x\text{Se}_{1-2x}$ glasses. Such experiments are currently ongoing and will be reported upon later.

In the Raman spectra, the appearance of vibrational modes of P_4S_4 and P_4S_3 monomers (containing P–P bonds, figure 5) at $x > 0.15$ is thus in harmony with these chemical considerations. P_4S_{10} and P_4S_7 monomers are terminated by singly coordinated $\text{P} = \text{S}$ species. These monomers occur with the S anion (but not with the Se anion), and are formed in the glasses starting from $x = 0.05$ to steadily increase in concentration with x to peak in the stressed-rigid glass compositions. And as one would expect on simple bond statistics [33], the S-rich monomer (P_4S_{10}) peaks (figure 6) at a lower x ($=0.13$) than the S-deficient (P_4S_7) one ($x = 0.18$).

As more P and Ge is alloyed in the glasses, one expects network fragments of amorphous P and amorphous Ge to emerge, as was recently observed in an examination of ternary $\text{Ge}_x\text{P}_x\text{Se}_{1-2x}$ glasses at $x > 0.20$ by Chakravarty [34]. Vibrational signatures of tetrahedrally coordinated P_4 clusters [27] (460 and 590 cm^{-1}) and an amorphous P [26] network (390 and 490 cm^{-1}) were observed in the selenides. In the present ternary, we do not have enough glass compositions at $x > 0.17$ to meaningfully elucidate these phases; however, we do observe a mode at 470 cm^{-1} in a sample at $x = 0.19$ which we assign to the presence of tetrahedral P_4 clusters in the present sulfides.

3.1.3. Glass transition temperature of a sulfur-chain glass. The magnitude of T_g contains vital structure information. The recognition emerged with the inception of stochastic agglomeration theory by Kerner and Micoulaut [35, 36]. In binary $(\text{T})_x\text{Se}_{1-x}$ glasses, where $\text{T} = \text{Si}$ or Ge , the variation of T_g with x is predicted [36] to be linear with a slope, dT_g/dx , of $T_0/\ln 4/2$; that is, independent of x in the stochastic limit (low $x \sim 5\%$). Here T_0 represents the T_g of Se glass, and the numbers of 4 and 2 represent the coordinations of Ge or Si and Se respectively. This prediction is in remarkable agreement [37] with experiments, and serves to underscore the notion that the magnitude of T_g serves as a good representation of network connectedness or mean coordination number \bar{r} . It is becoming increasingly clear that \bar{r} is an important topological factor necessary to understanding the physical behaviour [6] of disordered systems. The importance of chemical bond strengths in this respect is to serve as a scaling factor [38] in comparing networks having the same connectedness or mean \bar{r} .

In the present ternary sulfides, the increasing value of the glass transition temperature $T_g(x)$ with x constitutes a signature of an increase in network connectedness as P and Ge atoms cross-link S_n chains. The low value of T_g at $x = 0$ is most likely due to the absence of a network in the case of elemental S as mentioned earlier. The rapid increase of $T_g(x)$ at $x > 0.05$ is most likely due to the formation of a covalently bonded network of S_n chains mildly cross-linked by the P and Ge additives as the S_8 crown concentration vanishes (figure 2) near $x = 0.10$.

It is instructive to compare the $T_g(x)$ variation in the present ternary sulfides with the corresponding selenides [34], as illustrated in figure 7. In the $0.10 < x < 0.16$ range, one finds the variations in $T_g(x)$ for *both* ternaries (figure 7) to be strikingly parallel, with a scaling factor of 1.13. For example, at $x = 0.14$, we obtain a T_g in the ternary sulfide glass of 241°C or 514 K , and in a corresponding ternary selenide glass of 180°C or 453 K , yielding a scaling factor of $514\text{ K}/453\text{ K} = 1.13(1)$. The scaling reflects *similarities* of local structures of the backbones in the two chalcogenides in the $0.10 < x < 0.16$ range. The scaling factor can be traced to the higher bond strengths of Ge–S and P–S bonds in relation to Ge–Se and P–Se bonds. The Pauling single bond strengths (E_b), listed in table 2, reveal that the ratio

$$[E_b(\text{Ge-S}) + E_b(\text{P-S})]/[E_b(\text{Ge-Se}) + E_b(\text{P-Se})] = 1.10. \quad (3)$$

We thus find that the chemical bond strength scaling factor from equation (3) is in remarkable agreement with the T_g scaling factor of the glasses. These correlations serve to reinforce the topological or structural interpretation of T_g [37, 38] in network forming materials rather than the strictly chemical one advanced earlier [39].

The extrapolated value of T_g at $x = 0$ as shown by the dashed line in figure 7 in the present sulfide glasses gives a value of 115°C . This temperature then represents the predicted value of T_g of an S_n -chain glass based on the present work. Unfortunately, it is too close to the melting temperature of elemental sulfur and may well represent the basic limitation to form an S_n -chain glass.

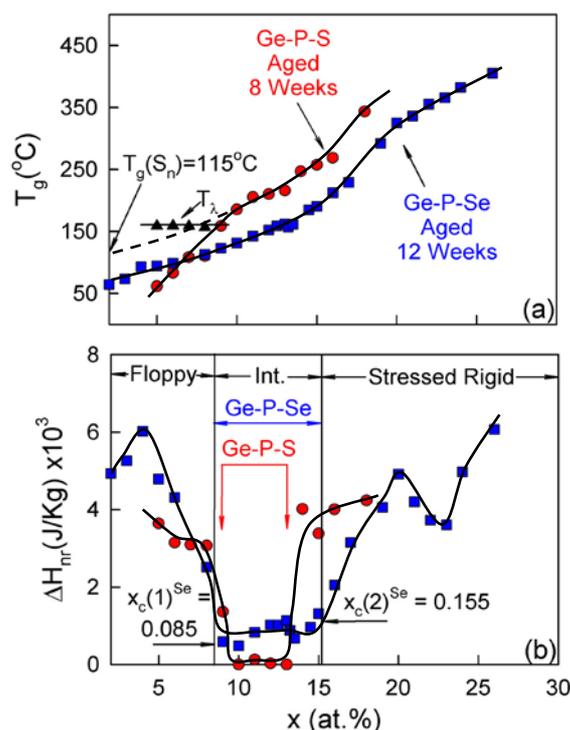


Figure 7. Compositional trends in (a) glass transition temperature (T_g) and (b) non-reversing heat flow (ΔH_{nr}) in $\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ glasses and corresponding $\text{Ge}_x\text{P}_x\text{Se}_{1-2x}$ glasses compared. The intermediate phase in the sulfide glasses narrows in relation to the selenides. The work on selenide glasses is taken from [34].

3.2. Elastic phases in $\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ glasses

The central result of the present study is the discovery of a *thermally reversing window* in the $0.09 < x < 0.135$ (figure 2) composition range. The result follows a pattern noted earlier [16, 40] in other chalcogenide glasses. In analogy to previous studies [8, 9, 16, 40], we identify glasses at $x < 0.09$ to be elastically *floppy*, those in the $0.09 < x < 0.135$ range to be in the *intermediate phase*, and those at $x > 0.135$ to be *stressed rigid*. Some of the physical characteristics of these elastic phases suggested from the present observations are discussed in the following discussion.

3.2.1. Elastically floppy phase ($x < 0.09$). The molecular structure of glasses at low x consists of S_8 crowns that segregate from a backbone of S_n chain fragments cross-linked by P-centred and Ge-centred local structures. The concentration of S_8 crowns is high at $x = 0.05$, but it steadily declines as x increases to 0.09. The non-reversing enthalpy of glasses in the floppy phase, ΔH_{nr} , displays a nearly symmetric peak that is about 25°C wide (figure 1(a)). Upon ageing, the ΔH_{nr} term increases by an order of magnitude (figure 1(a)), a feature that is tied to the mechanically under-constrained nature of S_n chains (table 3). In a chain, an S atom has one bond-stretching and one bond-bending constraints. Since the total count of constraints per sulfur atom of 2 is less than 3, the dimensionality of the network, $1/3$ of the vibrational modes are elastically floppy. Upon ageing, the chains flop around, increasing the entropy of the network;

Table 3. Mean co-ordination number, \bar{r} , and number of constraints per atom, n_c , of the network forming- and monomeric-units present in Ge–P–S glasses.

Unit	Mean co-ordination number (\bar{r})	No. of constraints/atom (n_c)	Comments
S ₈	2.00	2.00	Monomers; decouple from backbone. Presence inferred from their opening at the T_λ transition in MDSC scans.
QT S=P(S _{1/2}) ₃	2.29	3.00	Isostatic molecular units whose concentration peaks at $x = x_c(2) = 13\%$
P ₄ S ₁₀	2.29	3.00	Monomeric units present in the glasses beginning at very low values of x and highly populated around $x = 15\%$
P ₄ S ₇	2.36	3.09	Decoupled monomers appearing in glasses where $x > 14\%$
PYR P(S _{1/2}) ₃	2.40	3.00	Optimally constrained units forming part of backbone.
CS GeS ₄	2.40	3.00	Isostatic local structure forming part of the backbone. Their concentration is the highest when $\bar{r} = 2.40$ or x about 14%
P ₄ S ₄	2.50	3.25	Decoupled monomers; they begin to appear
P ₄ S ₃	2.57	3.43	in glasses when $x > 15\%$
ES GeS ₂	2.67	3.00	Isostatic local structures forming part of the backbone.
CS Ge(S _{1/2}) ₄	2.67	3.67	Stressed-rigid units present at $x > 13\%$ in glasses

this is reflected in an increase of ΔH_{nr} . Figure 1(a) also reveals that a sample at $x = 0.05$ ages much less than one at $x = 0.08$, we suppose because the fraction of S atoms present in the backbone in the former glass is minuscule in relation to that in the later glass. These results reinforce that the non-reversing enthalpy near T_g , ΔH_{nr} , is a backbone related property.

A comparison of the ΔH_{nr} term in Ge–P–Se and Ge–P–S glasses (figure 7) shows that at $x < 0.08$ the term ages much more in the selenides than in the sulfide glasses. Se-rich glasses are, in general, more polymerized than their S-rich counterparts, as alluded to earlier. The presence of pronounced ageing effects in the selenide glasses but its near absence in the sulfide glasses at low x underscores that the ΔH_{nr} term is intrinsically a backbone related property. In particular, monomeric units like S₈ or P₄S₁₀ that are decoupled from the network backbone apparently do not contribute to the non-reversing heat flow term.

3.2.2. Intermediate phase ($0.090 < x < 0.135$). The conditions leading a glass network to self-organize are very selective. A network must consist of local- and medium-range structures that are rigid but with no redundant bonds, i.e., it must be *isostatically rigid*. The presence of redundant bonds gives rise to stress and an increase in free energy. A network can lower its free energy by avoiding redundant bonds and forming a globally isostatically rigid backbone.

A covalent bond between two atoms provides a *bond-stretching* constraint that is shared equally between the two atoms. Thus, an atom having \bar{r} nearest-neighbours will have $\bar{r}/2$ bond-stretching constraints. In addition, there are $2\bar{r} - 3$ independent bond angles (in 3d) that must be specified to fix the local geometry of an atom having $\bar{r} (\geq 2)$ nearest neighbours, leading then to an equivalent number of *bond-bending* constraints. The total count of bonding

constraints [6, 7] then equals $(5\bar{r}/2 - 3)$, i.e., 7 for Ge ($\bar{r} = 4$), 2 for S ($\bar{r} = 2$) and 4.5 for P ($\bar{r} = 3$). For the special case of an atom having $\bar{r} = 1$, such as the terminal double bonded S in a QT ($\text{S}=\text{P}(\text{S}_{1/2})_3$) unit, one need count only 1/2 a bond-stretching constraint as discussed elsewhere [41–43].

Our Raman scattering results (figures 4(a)–(d)) reveal that the local structures present in the intermediate phase of the present glasses include CS- GeS_4 , ES- GeS_2 , PYR- $\text{P}(\text{S}_{1/2})_3$, QT- $\text{S}=\text{P}(\text{S}_{1/2})_3$. A count of *bond-stretching* and *bond-bending* constraints per atom for each of these local structures shows (table 3) a value of 3, exactly equal to the number of degrees of freedom of an atom in a 3d network. Thus, constraint counting algorithms demonstrate that these local structures are *isostatically rigid*. Furthermore, numerical simulations [44] also suggest that for these local structures to be part of a globally isostatically rigid backbone, they must form n -membered rings with $n \sim 6$. At present we are unable to address this aspect of structure from the local probe results at hand. However, it is possible that diffraction measurements [45] coupled with numerical simulations [46–48] may permit addressing this key issue of structure in the future. The width of the intermediate phase is broadly related to the range of chemical stoichiometries ($2.28 < \bar{r} < 2.67$) spanned by these local structures (figure 5). In the present ternary, the mean coordination number $\bar{r} = 2+3x$, and the intermediate phase of $0.090 < x < 0.135$ translates into the range $2.270 < \bar{r} < 2.405$, yielding a width of $\Delta\bar{r} = 0.135(15)$ in reasonable accord with these local structures.

An important feature of the intermediate phase glass compositions is that the non-reversing enthalpy is not only minuscule but that term apparently does not evolve in time, i.e., the glass network *does not age*. The backbone by virtue of an optimal connectedness exists in a state of equilibrium, and it appears that a consequence of that equilibrium is that these glasses do not age. The presence of a small but finite concentration of P_4S_{10} molecules (figure 6) in the intermediate phase attests to the robustness of the latter.

Recent Raman scattering experiments [49] on binary Ge–Se glasses performed as a function of hydrostatic pressure provide independent evidence that intermediate phase glass compositions exist in a state of equilibrium. The observation is related to the vanishing of the pressure threshold, P_c , in the intermediate phase but its presence in both floppy and stressed-rigid glass compositions. In these experiments, P_c serves as a measure of network internal stress that must be exceeded by an external pressure for the vibrational modes of a network to compress and blue-shift. The nature of medium range structures prevailing in such glasses that produce this remarkable equilibrium in a disordered network is the subject of ongoing investigations.

The intermediate phase in the Ge–P–Se ternary spans a range of $2.255 < \bar{r} < 2.465$, yielding a width [34] of $\Delta\bar{r} = 0.210(15)$, which is significantly larger than the one in the present sulfide glasses. The result is all the more interesting because the nature of the isostatic P- and Ge-centred local structures that contribute to self-organization in both ternaries shares much commonality. There are, however, some subtle differences of structure as well. For example, the P_4S_{10} and P_4S_7 monomers known to exist in the sulfides are apparently unstable with Se anions, we suppose because of the lower overlap of P d-orbitals with Se p-orbitals lowering the strength of the double bond. P_4S_{10} monomers persist in the intermediate phase (figure 6) at a low level, and are rapidly converted to their S-deficient counterparts, P_4S_7 monomers, in the $0.15 < x < 0.18$ range as the glasses become increasingly S-deficient. Furthermore, the appearance of P–P containing monomers P_4S_4 and P_4S_3 just above the window (figure 6), suggests that the network backbone must become depleted of the four isostatically rigid local structures as these monomers evolve once $x > 0.13$. We believe that these structure-related factors contribute to a down-shift of $x_c(2)$, the upper end of the window, from a value of 0.155(5) in the selenide to 0.135(5) in the corresponding sulfide glasses.

On the other hand, the lower edge of the intermediate phase is up-shifted from $x_c(1) = 0.085(5)$ in the $\text{Ge}_x\text{P}_x\text{Se}_{1-2x}$ ternary to $x_c(2) = 0.09(5)$ in the present $\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ ternary. Although the shift in the threshold is small, it is systematic and unmistakable (figure 7(b)). Its molecular origin is tied to the presence of S_8 rings that prevail at $x < 0.08$ and preclude a backbone forming, let alone becoming rigid. In the selenide glasses almost all the Se occurs in a polymeric form that promotes forming the backbone even at $x < 0.08$.

3.2.3. Stressed-rigid phase ($x > 0.135$). In the present glasses, the mode at 340 cm^{-1} has contributions from vibrational modes of several species including the CS tetrahedra of $\text{Ge}(\text{S}_{1/2})_4$ units. Some of these other species include P_4S_7 (346 cm^{-1}), P_4S_3 (342 cm^{-1}), and P_4S_4 (340 cm^{-1}), and each of these units contributes to the scattering near the 340 cm^{-1} mode once $x > 0.14$. For these reasons, it is not possible to infer the optical elasticity power-law [2, 3, 34] in the *stressed-rigid* glasses from a measurement of the 340 cm^{-1} mode frequency as a function of glass composition.

Important insights into the thermal behaviour of glasses in the *stressed-rigid* phase have emerged from the MDSC measurements [50]. The shape of the non-reversing heat flow near T_g in stressed-rigid glass compositions differs significantly from the one observed in floppy glass compositions; the exotherm is not only broad ($>50\text{ }^\circ\text{C}$) but also has an asymmetrical shape—a tail that extends to temperatures well above T_g . It appears that structural arrest in such systems occurs at a temperature well above T_g , we suppose because the network is mechanically overconstrained. In this composition range, the backbone consists of corner-sharing $\text{Ge}(\text{S}_{1/2})_4$ tetrahedral units that are overconstrained in that they possess a count of bonding constraints of 3.67 per atom (table 3) that exceeds the threshold value of 3 coming from the 3d nature of the backbone.

Our results in the *stressed-rigid* glass compositions are limited, because we were unable to obtain homogeneous glasses at $x > 0.19$ in the present sulfides. The result is not entirely unexpected given the proliferation of molecular phase separation discussed above. But in the corresponding ternary selenides [34], where such effects are qualitatively absent, many more glass compositions could be synthesized and examined by Raman scattering. These results show that modes of tetrahedral P_4 and amorphous P evolve at higher x in the selenides. And one expects a qualitatively similar behaviour to occur in the present sulfides.

4. Nanoscale phase separation and self-organization effects in ternary Ge–P–S glasses

The Ge–P–S ternary displays an extensive glass forming region sketched in figure 8 taken from [51]. The glass compositions studied in the present work reside along the bisector of the P–S–Ge angle in the composition triangle. The thermal behaviour and molecular structure of binary P_xS_{1-x} glasses were examined in NMR, Raman scattering and DSC measurements by Eckert *et al* [22, 23], who noted the existence of a global maximum in T_g near $x \sim 0.20$ (figure 9). Their NMR results showed binary glass compositions at $x > 0.20$ to be composed of P_4S_n monomers with $n = 7, 10$, i.e. nanoscale phase separated. Glass compositions along the P_2S_5 – GeS_2 join (shown by open (brown) squares in figure 8) were examined in ^{31}P NMR, Raman scattering and DSC measurements by Cherry *et al* [52]. In a separate study, the same authors examined ternary $\text{Ge}_{0.714x}\text{P}_{0.286x}\text{S}_{1-x}$ glasses (open (blue) triangles in figure 8) in ^{31}P NMR, Raman scattering, DSC and neutron elastic measurements [53]. These latter glasses differ from the one examined presently in that the Ge/P cation ratio is 2.5 instead of 1. Of interest is the fact that the glass transition temperatures, $T_g(x)$, increase with x to show a threshold near $x = 1/3$ (figure 9) and to decrease thereafter ($x > 1/3$). The behaviour is

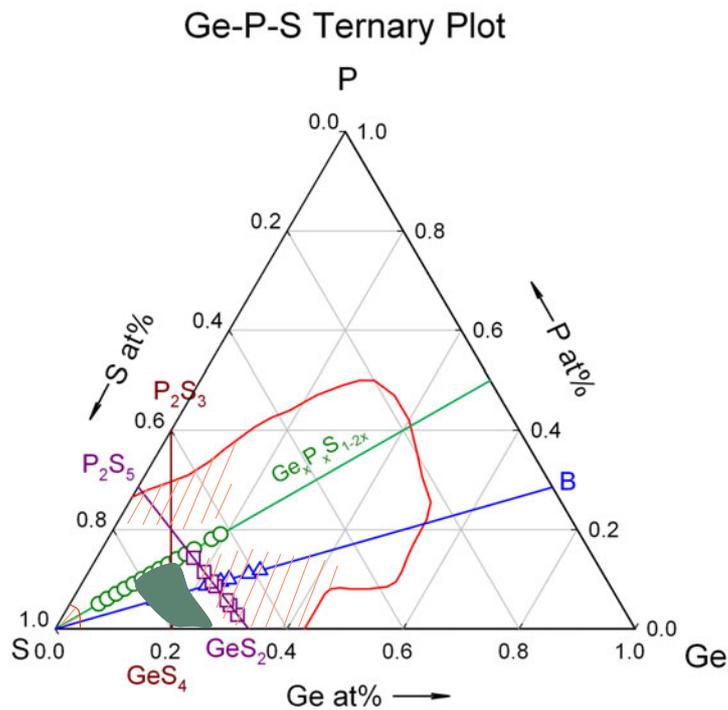


Figure 8. Glass forming region in the Ge–P–S ternary depicting the glass composition studied presently (open (green) circles). Blue triangle and brown square compositions were studied in [52] and [53] respectively. The shaded (green) region indicates glasses that are self-organized while the red-hashed region glass compositions that are nanoscale phase separated.

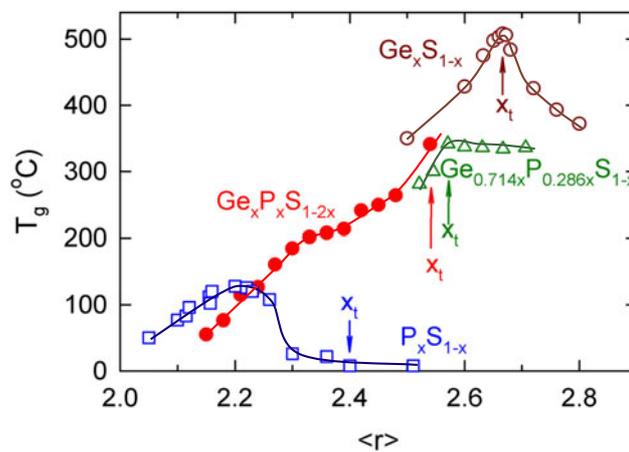


Figure 9. Compositional trends in glass transition temperatures in $\text{Ge}_x\text{S}_{1-x}$, P_xS_{1-x} , $\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ and $\text{Ge}_{0.714x}\text{P}_{0.286x}\text{S}_{1-x}$ glasses plotted as a function of mean co-ordination number r . The arrows mark the mean co-ordination number r at which the chemical threshold x_t occurs in these glass systems.

reminiscent of the one encountered in binary $\text{Ge}_x\text{S}_{1-x}$ glasses [54] near the chemical threshold of $x_t = 1/3$, which constitutes evidence for nanoscale phase separation [38] of a Ge-rich phase

(containing Ge–Ge bonds) from the $\text{Ge}(\text{S}_{1/2})_4$ backbone once $x > x_t$. These nanoscale phase separation effects can be qualitatively suppressed when the Ge/P ratio equals 1, as reflected in the monotonic increase of $T_g(x)$ observed in the present glasses (figure 9). The pattern is not unique to the present Ge–P–S ternary but has been observed in other ternaries such as Ge–P–Se, Ge–As–Se, Ge–As–S as discussed elsewhere [38]. Spectroscopic probes such as Raman scattering, NMR, Mossbauer effect, provide powerful probes of local structure in glasses. However, from a measurement at one glass composition it is generally impossible to tell if these local structures form part of the same backbone or are formed in separate molecular clusters or backbones. In this latter respect, variations in T_g with glass composition have turned out to be decisive, as discussed elsewhere [38, 54]. The intrinsically nanoscale phase separated regions are shown with hashed lines in figure 8.

The intermediate phase established in the present ternary glasses along with our tentative estimate of this phase in the Ge–S binary is sketched green in figure 8. The intermediate phase in Ge–S glasses has not been firmly established, although its light-induced collapse at the mean-field rigidity transition has been observed [4]. Currently, there is no information on the existence of the intermediate phase in the P–S binary.

One cannot help but comment on the robustness of the intermediate phase in the present $\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ ternary glasses. In the intermediate phase, we observe evidence of the four isostatic local structures that form the building blocks of the stress-free backbone alluded to earlier. In addition, we also observe evidence of a small (<5 mol%) but finite concentration of P_4S_{10} monomers in this phase. And apparently, this small concentration of monomers does not influence the non-ageing behaviour of the intermediate phase up to 8 weeks. It is of interest to examine the location of the intermediate phase in the P–S and Ge–S binaries unambiguously and to establish the phase boundaries of the three elastic phases in these ternary glasses as was done in the corresponding selenide glasses [2].

5. Conclusions

In the present work, we have examined ternary $\text{Ge}_x\text{P}_x\text{S}_{1-2x}$ glasses over a wide composition range, $0.05 \leq x \leq 0.19$, using Raman scattering and MDSC experiments. The latter experiments show the existence of a *thermally reversing window* in the $0.09 < x < 0.135$ range. The observation suggests that glasses at $x < 0.09$ are elastically floppy, and those in the $0.09 < x < 0.135$ are in the intermediate phase, while those at $x > 0.135$ are stressed-rigid. Furthermore, the MDSC experiments reveal that for glass compositions in the intermediate phase, not only is the non-reversing heat flow term, ΔH_{nr} , minuscule (~ 0) but that term does not age for a waiting time of 8 weeks. In stressed-rigid and floppy glass compositions, the ΔH_{nr} term is not only an order of magnitude larger but the term is found to age. Raman scattering experiments show that there are four isostatic local structures including CS-GeS_4 , ES-GeS_2 , $\text{PYR-P}(\text{S}_{1/2})_3$, $\text{QT-S=P}(\text{S}_{1/2})_3$ populated in the intermediate phase. The width of the intermediate phase in the present ternary sulfides of $\Delta\bar{r} = 0.135(15)$ is significantly narrower than in the corresponding selenides ($\Delta\bar{r} = 0.210(15)$). The narrower intermediate phase width in the sulfides in relation to the selenide glasses is ascribed to the presence of nanoscale phase separation of S_8 monomers in the floppy phase, and P_4S_4 and P_4S_7 monomers in the stressed-rigid phase that suppress the formation of a backbone in which rigidity could percolate.

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