

# Origin of Conductivity Threshold in the Solid Electrolyte Glass System: $(\text{Ag}_2\text{S})_x(\text{As}_2\text{S}_3)_{1-x}$

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**Abstract**—The electrical conductivity of  $(\text{Ag}_2\text{S})_x(\text{As}_2\text{S}_3)_{1-x}$  glasses increases to display a step-like jump of nearly five orders of magnitude in the narrow composition range,  $9\% < x < 15\%$  range. To elucidate the origin of this threshold behavior, we have now examined the molecular structure of these glasses in modulated-differential scanning calorimetry (MDSC) and Raman scattering experiments. Our MDSC results reveal bimodal glass transition temperatures ( $T_g$ s), a low- $T_g$  and a high- $T_g$  in the  $7\% < x < 40\%$  range but unimodal ones outside this range. The low- $T_g$  phase bears a similarity to that of the stoichiometric glass at  $x = 1/2$ , or  $\text{AgAsS}_2$ , and we identify it with a Ag-rich phase formed in these glasses once  $x > 7\%$ . The Ag-rich phase is thought to percolate near  $x \sim 9\%$ , and to contribute to the large jump in conductivity of the glasses. The high- $T_g$  phase represents a semiconducting  $\text{As}_2\text{S}_3$  glass phase alloyed with a few mole percent of  $\text{Ag}_2\text{S}$ , and it displays a reversibility window in the  $8\% < x < 13\%$  range. The semiconducting phase becomes elastically flexible once  $x > 13\%$ . Softening of the high- $T_g$  phase lowers  $\text{Ag}^+$  ion migration energies and also contributes to the conductivity threshold.

**Index Terms**—Macroscopic phase separation, modulated DSC, Raman scattering, self-organization, solid electrolyte glasses.

## I. INTRODUCTION

**A**DDITION of the solid electrolytes,  $\text{Ag}_2\text{S}$ ,  $\text{Ag}_2\text{Se}$ , and  $\text{AgI}$  to base oxide- and/or chalcogenide glasses has been examined for the past two decades. Interest in these materials stems from their increased ionic conductivity [1] with progressive alloying of the solid electrolyte additive. Solid electrolyte glasses have found applications as sensors, as electrolytes for batteries, and as materials for electrochromic displays [2]. At a basic level, the increase in conductivity with chemical composition continues to be a subject of ongoing discussions in the field. In some cases, the conductivity displays a gradual increase [3] with the solid electrolyte content. In other cases, one observes [4] a threshold reminiscent of a percolative behavior. In spite of these details, one continues to remain uncertain over the nature of the percolating species. The present glass system has received particular attention in this respect, and evidence [1], [5] of a giant increase of conductivity has been observed when  $x$  increases to  $\sim 15\%$  as shown in Fig. 1. At  $x \sim 5\%$ , the electrical conductivity is characteristic of a semiconducting glass, while at  $x > 15\%$ , it is representative of an ionic conductor.

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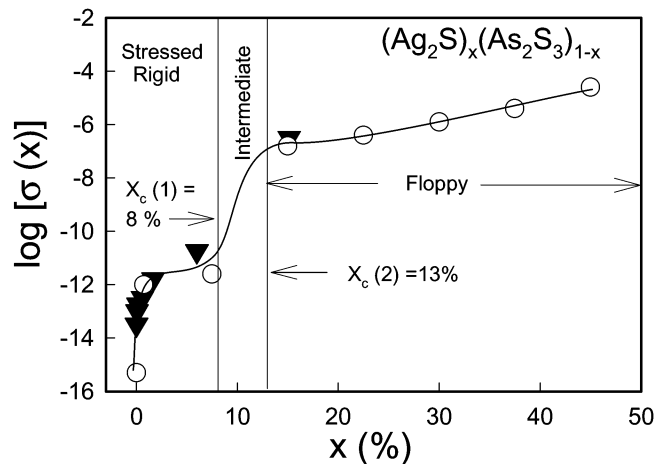


Fig. 1. Electrical conductivity  $\sigma(x)$  of titled glasses showing a threshold behavior near  $x \sim 0.10$ . The open circle (o) results are taken from [1], while the filled triangle ( $\blacktriangledown$ ) results are from [11]. The three phase identification shown above is inferred from the present work. See text.

Solid electrolytes such as  $\text{AgI}$ ,  $\text{Ag}_2\text{S}$ ,  $\text{Ag}_2\text{Se}$  can exist in a glassy phase as additives to base chalcogenide glasses. The realization first emerged [6] from scanning calorimetric measurements that have revealed bimodal glass transition temperatures. In select cases, one  $T_g$  comes from the base glass while the other from a Ag-rich glass phase. Theoretical support for these ideas on phase separation have come from constraint counting algorithms that have permitted correlating the magnitude of observed  $T_g$ s to the connectedness of the glassy networks [6]. Recently one has found [7] that when Ag is alloyed in S-rich ( $x < 1/3$ )  $\text{Ge}_x\text{S}_{1-x}$  glasses, bimodal glass transitions ( $T_g$ s) are observed. In these experiments, one of the  $T_g$ s near  $320^\circ\text{C}$  is ascribed to an  $\text{Ag}_2\text{S}$ -rich glass phase while the other to the S-deficient base  $\text{Ge}_t\text{S}_{1-t}$  glass phase in analogy to previous work on corresponding selenides [8]. Fundamentally, such macroscopic phase separation is driven by free energy considerations; instead of having a fully polymerized network of a high connectedness and thus high free energies, glasses intrinsically segregate into two separate phases of lower connectedness possessing lower free energies.

Given these ideas on macroscopic phase separation, it is also of interest to inquire when might one of these phases percolate and contribute to a giant conductivity enhancement. Consider, for example, a heterogeneous glass system composed of two glass phases: a conducting one and an insulating one. Imagine steadily increasing the fraction of the conducting phase by chemical alloying. When might one expect conducting glass phase to percolate? The issue was addressed several years ago by H. Scher and R. Zallen [9], who showed that percolation of the minority phase will occur, in general, when its volume

fraction approaches a threshold value of 1/6 or 16.6%. These basic ideas on scalar percolation are relevant to the present work as we will illustrate to understand electrical transport and structure of the present glasses.

The present  $(\text{Ag}_2\text{S})_x(\text{As}_2\text{S}_3)_{1-x}$  glass system has been the subject of several previous investigations, including elastic neutron scattering [10], small angle neutron scattering [11], EXAFS [12], Raman scattering [12], field emission SEM [13], and differential scanning calorimetry [11]. In spite of these detailed investigations, a general understanding of features of structure that contribute to the giant enhancement of conductivity in a narrow composition range  $10\% < x < 15\%$  of  $\text{Ag}_2\text{S}$  has remained largely elusive. In some of these studies [11], [13], macroscopic phase separation of these glasses was recognized, but the nature of the underlying phases and their role in relation to conductivity enhancement was not obvious.

In the present work we have synthesized  $(\text{Ag}_2\text{S})_x(\text{As}_2\text{S}_3)_{1-x}$  glasses over a wide concentration range,  $0\% < x < 80\%$ , and have examined them in modulated differential scanning calorimetry (MDSC) and Raman scattering experiments. We show that these glasses are intrinsically phase separated on a macroscopic scale in the  $8\% < x < 40\%$  range into two bulk glass phases, and such a behavior plays a central role in understanding the giant enhancement of electrical conductivity in the  $10\% < x < 15\%$  range. Our results suggest that one of these phases is a Ag-rich phase based largely on the structure of the  $x = 50\%$  glass. The second glass phase is the base glass and it is softened by the  $\text{Ag}_2\text{S}$  additive, and it then also contributes to the conductivity enhancement. The rest of the paper is organized as follows. In Section II, we present experimental results. This is followed by Section III in which we discuss these results. A summary of conclusions emerging from the present work is given in Section IV.

## II. EXPERIMENTAL

### A. Synthesis of Glasses

High purity (99.999%) Ag, S, and  $\text{As}_2\text{S}_3$  from Cerac Inc., were used as starting materials to synthesize the glasses. Elemental Ag was heated in air to  $550^\circ\text{C}$  to remove traces of surface oxidation. Ag and S were first reacted in evacuated ( $2 \times 10^{-7}$  torr) quartz ampoules to synthesize crystalline  $\text{Ag}_2\text{S}$ . The product displayed the characteristic  $\beta \rightarrow \alpha$  crystalline phase transition onset near  $175^\circ\text{C}$  in harmony with published reports [14].  $\text{Ag}_2\text{S}$  and  $\text{As}_2\text{S}_3$  were then mixed in the appropriate ratios by weight to prepare bulk glasses of the desired composition  $x$ . The starting materials were reacted at  $950^\circ\text{C}$  for 48 h, and melt temperatures were then lowered to  $50^\circ\text{C}$  above the liquidus for several hours before a water quench. Once synthesized glasses were stored in evacuated pyrex tubings. All sample handling was performed in a glove box purged with dry nitrogen gas.

### B. Modulated DSC Results

A model 2920 Temperature Modulating DSC (MDSC) from TA Instruments Inc. was used to establish glass transition properties. All scans mentioned in this work were taken at a  $3^\circ\text{C}/\text{min}$  scan rate and  $1^\circ\text{C}/100\text{ s}$  modulation rate. Typically a sample was heated starting  $50^\circ\text{C}$  below  $T_g$ , and taken up in temperature to  $50^\circ\text{C}$  above  $T_g$ . The temperature of the calorimeter was then

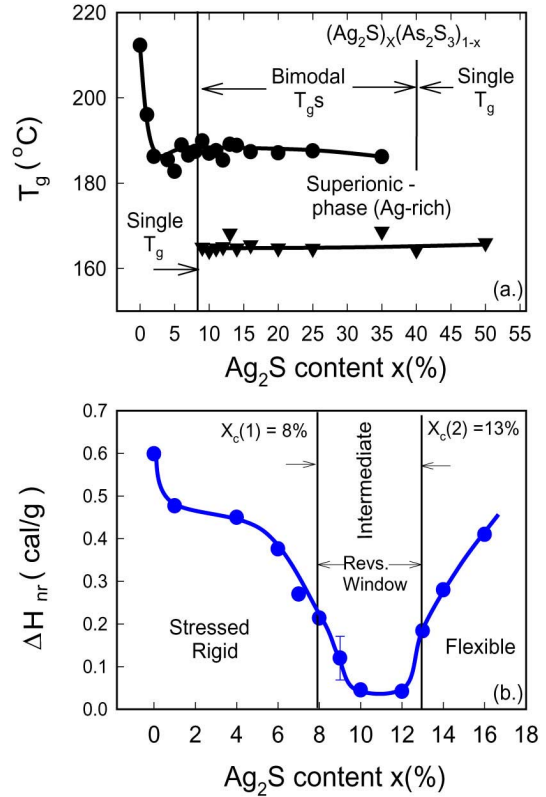


Fig. 2. Compositional variations of: (a) glass transition temperature  $T_g(x)$  and (b) the nonreversing enthalpy  $\Delta H_{nr}(x)$  in titled glasses. Single  $T_g$ s are observed at  $x < 8\%$  and at  $x > 40\%$ , but two  $T_g$ s appear in the  $8\% < x < 40\%$  intervening region. The global minimum in  $\Delta H_{nr}(x)$  serves to define the intermediate phase of the high- $T_g$  phase.

lowered to the starting temperature to record all the heat flow signals in a cool down past the glass transition. The advantage [15] of MDSC over conventional DSC is that it is a far more sensitive instrument and it permits deconvoluting the heat flow endotherm into a reversing and a nonreversing component. Glass transition temperatures ( $T_g$ s) are precisely determined from the inflection point of the reversing heat flow. The nonreversing enthalpy ( $\Delta H_{nr}$ ) associated with  $T_g$  is deduced by integrating the area under the Gaussian-like peak observed in the nonreversing heat flow signal. A frequency correction [16] to the nonreversing enthalpy  $\Delta H_{nr}$  is made by subtracting the  $\Delta H_{nr}$  term measured upon cool down from the term measured upon heating.

A summary of MDSC results appears in Fig. 2. In general, a solitary  $T_g$  is observed at  $x < 7\%$ , but two  $T_g$ s are observed in the  $7\% < x < 40\%$  range, followed by a single  $T_g$  at higher  $x$  ( $> 40\%$ ). We note that there is a sharp reduction in the value of glass transition temperature of the semiconducting (high- $T_g$ ) phase upon alloying a few percent of  $\text{Ag}_2\text{S}$ . Thereafter,  $T_g$ s of this phase more or less saturate to a value of about  $186^\circ\text{C}$  independent of  $x$ . The  $T_g$  of the low- $T_g$  phase remains more or less independent of  $x$  and has a value of  $168^\circ\text{C}$ . In Fig. 2(b), we summarize compositional trends in the  $\Delta H_{nr}(x)$  term, and find evidence of a global minimum in the  $8\% < x < 13\%$  range. Such minima have been observed earlier in chalcogenide glasses and are known to represent the reversibility window [17], [18]. In these windows glass transitions become thermally reversing in character, a feature that is identified with self-organized networks [18] as we shall discuss later.

Glass forming tendency in the present ternary extends up to  $x \sim 75\%$ . The chemical composition  $x = 50\%$  corresponds to the stoichiometric composition  $\text{AgAsS}_2$ , which is also known to exist as a crystalline compound known as Smithite [12]. The stoichiometric composition can be readily vitrified. We have synthesized the  $x = 50\%$  glass and have obtained a  $T_g$  of  $166^\circ\text{C}$ . We note that this value of  $T_g$  is characteristic of the low- $T_g$  phase present in the ternary glasses once  $x$  exceeds approximately 10% [Fig. 2(a)].

The specific heat jump near  $T_g$  provides in good measure the concentration of a glass phase. The specific heat jump ( $\Delta C_p$ ) at the glass transition for both the low- $T_g$  and high- $T_g$  phases were measured by analyzing the reversing heat flow signals. From MDSC scans, we measure  $\Delta C_p$  (low- $T_g$ ) and  $\Delta C_p$  (high- $T_g$ ) and obtain the ratio  $R$  defined as

$$R = \frac{\Delta C_p(\text{low-}T_g)}{[\Delta C_p(\text{low-}T_g) + \Delta C_p(\text{high-}T_g)]}. \quad (1a)$$

The quantity  $R$  provides a measure of the fraction of the low- $T_g$  phase in the glasses. We note that the fraction  $R(x)$  is vanishing at  $x = 7\%$ , but it increases sharply in the  $7\% < x < 9\%$  range. A plateau sets in the  $9\% < x < 13\%$  range. Thereafter,  $R(x)$  increases linearly to acquire a value of 100% near  $x = 40\%$ . We have also measured the molar volumes ( $V_m$ ) of glasses, and find  $V_m(g - \text{As}_2\text{S}_3) = 16.0 \text{ cm}^3/\text{mol}$  and  $V_m(g - \text{AgAsS}_2) = 14.74 \text{ cm}^3/\text{mol}$ . Using these data we have calculated the volume fraction,  $V(x)$ , of the low- $T_g$  phase using the relation (1b),

$$V(x) = \frac{A}{B} \quad (1b)$$

where

$$A = \Delta C_p(\text{low-}T_g)V_m(g - \text{AgAsS}_2),$$

and

$$B = [\Delta C_p(\text{low-}T_g)V_m(g - \text{AgAsS}_2) + \Delta C_p(\text{high-}T_g)V_m(g - \text{As}_2\text{S}_3)].$$

A plot of  $V(x)$  appears in Fig. 3. One finds that in the composition range of  $8\% < x < 13\%$ , corresponding to the reversibility window,  $V(x)$  takes on a value of about 16% and remains unchanged. An enlarged view of the rectangular region of Fig. 3(a) is displayed in Fig. 3(b). The threshold compositions,  $x_c(1)$  and  $x_c(2)$ , represent respectively the stress- and rigidity-transition. Also shown in Fig. 3(b) is the special composition  $x = x_{SZ} = 9\%$  where  $V(x)$  acquires a value of 16%, the Scher-Zallen threshold [9]. At  $x > x_{SZ}$ , one expects the low- $T_g$  phase to percolate and electrical conductivity to abruptly increase. We shall return to discuss these results in Section III.

### C. Raman Scattering

A Thermo-Nicolet FTIR Research grade bench with a Raman module was used to record FT-Raman spectra of glass samples. An advantage of exciting the scattering in the red instead of the visible light is that one can minimize photostructural effects [19] associated with Ag-photodiffusion in these Ag-bearing glasses. The  $1.06 \mu\text{m}$  laser beam was brought to a loose focus ( $50 \mu\text{m}$  spot size) on samples. In these experiments the incoming beam comes to a line focus on samples because of the cylindrical shape of the quartz tubing encapsulating them. Such geometry

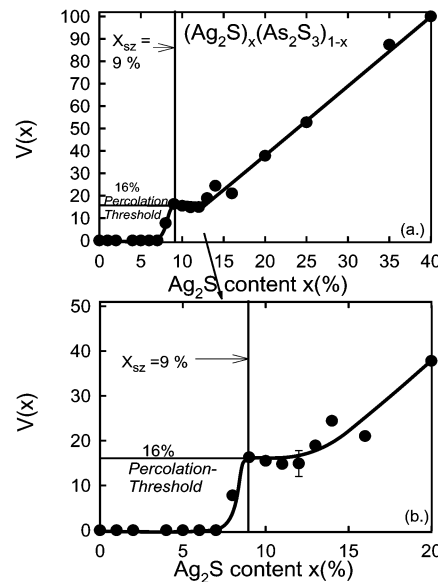


Fig. 3. (a) Plot of  $V(x)$ , volume fraction of the low- $T_g$  glass phase. It displays a general increase as the  $\text{Ag}_2\text{S}$  content increases in the present  $(\text{Ag}_2\text{S})_x(\text{As}_2\text{S}_3)_{1-x}$  glasses. (b) Magnified view of the rectangular region of (a). It shows the  $V(x)$  to approach the Scher-Zallen value of 16% when the glass composition acquires a value of  $x = 9\%$ . See text for details.

further lowers, substantially, the laser power density on samples. The typical power used in these experiments was 100 mW, and an acquisition used 300 cycles resulting in an instrumental resolution of  $1 \text{ cm}^{-1}$ . At these low power densities, we could not detect any light-induced effects. The observed lineshapes are thought to represent the intrinsic vibrational density of states in the glasses.

Fig. 4 provides a summary of the Raman scattering results on the present glasses displayed systematically with increasing  $\text{Ag}_2\text{S}$  content  $x$ . The observed lineshape of a glass sample at  $x = 10\%$  is found to be quite similar to the one reported [12], [20] for pristine  $\text{As}_2\text{S}_3$  glass at  $x = 0\%$ . Several groups have examined [12], [20] this particular glass and a fairly good understanding of the vibrational modes have emerged from the recent work of Georgiev *et al.* [20] The narrow features near  $180 \text{ cm}^{-1}$  and  $220 \text{ cm}^{-1}$  labeled R are identified with Realgar ( $\text{As}_4\text{S}_4$ ) molecules. These molecules segregate from the backbone even in the base glass. In the present glasses, with steadily increasing concentration  $x$ , we observe two new features in the spectra; Realgar molecules consistently nanoscale phase separate as  $x$  increases to 35%. Concomitantly, a broad mode (labeled as S for Smithite) centered near  $375 \text{ cm}^{-1}$  begins to manifest, and its presence broadens the main band centered near  $350 \text{ cm}^{-1}$  of  $\text{As}_2\text{S}_3$  glass. At  $x > 35\%$ , the Smithite-mode manifests as a shoulder to the  $350 \text{ cm}^{-1}$  band. At  $x = 50\%$ , it becomes the principal feature of the present ternary glasses.

Broadly speaking, features observed in Raman scattering of the present glasses in the  $150 \text{ cm}^{-1} < \nu < 500 \text{ cm}^{-1}$  range, largely emerge from vibrations associated with As-S bonds. Scattering from Ag-S bonds is not only much weaker in strength but also it is shifted to lower frequencies ( $< 150 \text{ cm}^{-1}$ ). Several groups [5], [12] have reported Raman scattering of the stoichiometric  $\text{AgAsS}_2$  glass. Our result for the stoichiometric glass ( $x = 50\%$ ) in Fig. 4 is in harmony with these earlier reports. The main feature at  $375 \text{ cm}^{-1}$  in the stoichiometric glass can readily

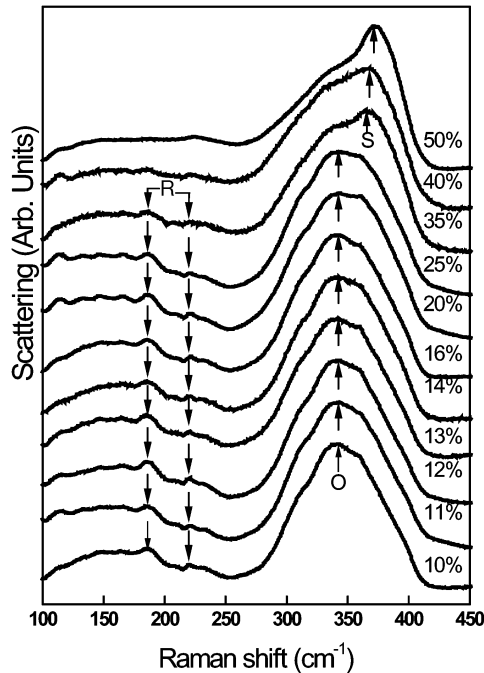


Fig. 4. Raman scattering in  $(\text{Ag}_2\text{S})_x(\text{As}_2\text{S}_3)_{1-x}$  glasses at indicated glass compositions  $x$ . The mode labeled S near  $375\text{ cm}^{-1}$  is characteristic of the 50% glass. This mode is observed in glasses at  $x = 25\%$ ,  $35\%$ ,  $50\%$ . It contributes to the high frequency shoulder of the main band centered near  $350\text{ cm}^{-1}$ . The main band comes from Orpiment-like phase (O) of the base glass composed of 12-membered rings. The modes near  $180$  to  $250\text{ cm}^{-1}$  labeled R come from  $\text{As}_4\text{S}_4$  molecules characteristic of Realgar [20].

be identified [5] with the symmetric stretch of As–S modes in  $\text{AsS}_3$  pyramids present in 6-membered rings. A 6-membered ring is made up of 3 pyramidal units. The main band in  $\text{As}_2\text{S}_3$  glass is observed near  $350\text{ cm}^{-1}$ , i.e., it is shifted to a lower frequency. We believe this shift comes from  $\text{AsS}_3$  pyramids present in rings that have 12 members or 6  $\text{AsS}_3$  pyramids. The blue shift of the mode in question with decreasing ring size is a fairly general feature observed in other glass systems [16]. The blue shift is due to pyramids becoming more stressed in rings of a smaller size as intramolecular interactions grow at the expense of intermolecular ones.

We have also examined Raman scattering from c- $\text{AgAsS}_2$  (Smithite) as a function of increasing laser power density. In these experiments, we are able to observe the vibrational modes to steadily broaden and to acquire features characteristic of the glass as the laser power density increases. Light-induced vitrification of Smithite illustrates that the spectrum of the glass (in Fig. 4) evolves smoothly and almost continuously from that of the crystal. These results will be presented elsewhere. Next we shall discuss the structure implications of the Raman scattering and MDSC results next.

### III. DISCUSSION

There is broad recognition that Ag in glasses readily photodiffuses [21]. Indeed, applications of spectroscopies that use a beam of visible light or an electron beam to probe structure of Ag-based glasses has always been problematic; one runs the risk of altering Ag-centered local structures in the very process of probing them if the flux of incident beam is high. These limitations are much less severe in using thermal methods to probe

glass structure. It is in this respect that MDSC serves as an important check on interpretation of results from more traditional techniques. Use of MDSC as a probe of glass structure through measurements of the reversing heat flow (related to ergodic processes and thermodynamic parameters such as  $T_g$  and  $\Delta C_p$ ) and the nonreversing enthalpy (nonergodic processes related to structural arrest) has proved to be quite rewarding as discussed in recent reviews [18], [22]. In DSC experiments one is forced to use higher scan rates (20 K/min) than in MDSC ones (3 K/min) because of the lower sensitivity of the former (dc) versus the latter (ac) method. This limitation leads to kinetic shifts in the glass transition temperature in the former but not the latter method. Furthermore, in DSC experiments one infers  $T_g$  and  $\Delta C_p$  from the total heat flow. This has the obvious limitation that ergodic processes that control these thermodynamic parameters are polluted by nonergodic ones.

#### A. Macroscopic Phase Separation of $(\text{Ag}_2\text{S})_x(\text{As}_2\text{S}_3)_{1-x}$ Glasses

The bimodal glass transition temperatures observed in the present work (Fig. 2) confirm the earlier findings of Bychkov *et al.* [11] that the present glasses, in the  $7\% < x < 25\%$  composition range, are segregated on a macroscopic scale. Macroscopic phase separation of glasses in this composition range is independently corroborated by small angle neutron scattering results [11] which reveal two orders of magnitude higher scattering at  $q = 0.002\text{ \AA}^{-1}$  in a glass at  $x = 16.6\%$  than at  $x = 1.8\%$  or even at  $x = 37.5\%$ . A detailed comparison of compositional variations in  $T_g$  of the two phases is summarized in Fig. 2(a). These results are quite similar to those reported earlier [11]. Small differences in  $T_g$  trends between the present results and those of Bychkov [11], most likely, result from the use of MDSC by us and DSC by them. For example, in the present work the region of bimodal glass transition temperatures ( $7\% < x < 40\%$ ) is wider than the one reported by Bychkov [11] ( $8\% < x < 25\%$ ).

#### B. Identification of the High- $T_g$ Phase

The high- $T_g$  phase represents the base semiconducting  $\text{As}_2\text{S}_3$  glass alloyed with a few mole percent of the  $\text{Ag}_2\text{S}$  additive. The sharp drop in  $T_g$  of this phase probably comes from weaker Ag–S bonds replacing stronger As–S bonds as Ag replaces As in the backbone interior with a coordination number of 3. Some of the Ag probably also segregates to internal surfaces of the glass to be fourfold coordinated with three bridging S near neighbors forming part of the backbone and a nonbridging  $\text{S}^-$  thio unit as a dangling end. Ag has a covalent radius of 1.34 Å, which is about 12% larger than that of As (1.20 Å). The free energy of the alloyed glass will be lowered by segregation of the oversized cation to internal surfaces. Such a fourfold coordination could be compatible with the neutron scattering results of Penfold and Salmon [10] who claim to find evidence for fourfold coordinated Ag at  $x = 9.6\%$ . The diffraction result must be treated with caution because a ternary glass at  $x = 9.6\%$  was treated by Penfold and Salmon as a homogeneous glass with a  $T_g$  of  $180\text{ }^\circ\text{C}$ .

#### C. Identification of the Low- $T_g$ Phase

The low- $T_g$  phase first nucleates once  $x > 7\%$ , and it grows precipitously with increasing concentration of  $\text{Ag}_2\text{S}$ . Its  $T_g$  then becomes quite similar to that of the stoichiometric glass at  $x =$

50%. Once  $x$  approaches about 8%, the  $\text{Ag}_2\text{S}$  additive nucleates a Ag-rich low- $T_g$  glass phase instead of alloying in the base glass (high- $T_g$ ) phase. We suppose this is the case because replacement of As by the oversized Ag leads to accumulation of strain. On the other hand, macroscopic phase separation lowers the free energy by creating two types of glass phases that are optimally connected. Once the low- $T_g$  phase nucleates, it appears that some of the Ag from the (stressed) high- $T_g$  phase moves over to the low- $T_g$  phase. The signature of this shift of Ag to the high- $T_g$  phase is the mild increase of  $T_g$  of that phase once  $x > 5\%$ . The observation of a low  $T_g$  glass transition once  $x > 7\%$  suggests that the spatial extent of the Ag-rich phase must be in the micrometer range. And it is possible that at  $x < 7\%$ , a precursor to the low  $T_g$  phase observed (at  $x > 7\%$ ) exists in the present glasses. However, the absence of a low- $T_g$  glass transition at  $x < 7\%$  would simply place the spatial extent of such a Ag-rich phase to be less than submicron dimensions.

The structure of Smithite is remarkable in many ways. It is made up of  $\text{As}(\text{S}_{1/2})_3$  pyramids present in 3 membered rings that share 3  $\text{Ag}^+$  compensating cations. The mean coordination number,  $r$ , of the network can be calculated by taking the coordination numbers of Ag, As, and S to be respectively 3, 3, and 2. Calculations reveal  $r = 2.5$ , corresponding to the count of Lagrangian constraints due to bond-stretching and bond-bending forces per atom of  $n_c = 3.25$ . Furthermore, if Ag is mobile in the structure as is suggested from conductivity measurements, then it can be shown that the count of mechanical constraints per atom ( $n_c$ ) associated with the network reduces to  $n_c = 2.50$ . The magic value of  $n_c$  for the glass forming tendency to be optimized [23] according to J. C. Phillips is  $n_c = 3$ . It is, therefore, not a surprise that the molecular structure of Smithite lends itself to easy glass formation. The low- $T_g$  glass phase formed in the present glasses near the composition  $x = 25\%$ , probably consist of rings that are closer to 6 (as in orpiment) rather than 3 as in Smithite. In the  $35\% < x < 50\%$  composition range, one may write the approximate chemical stoichiometry of the low- $T_g$  phase to be  $(\text{As}_2\text{S}_3)_x(\text{Ag}_2\text{S})_{1-x}$  with  $x$  in the  $1/3 < x < 1/2$  range. Since both Ag and As are threefold coordinated, the mean coordination number  $r$  and therefore  $T_g$ s remain largely independent of  $x$ . The coordination of Ag of 3 in the Smithite glass is consistent with the neutron scattering results of Penfold and Salmon [10].

#### D. Conductivity Threshold and Scher–Zallen Percolation of the Low- $T_g$ Phase

The macroscopic segregation of the present ternary glasses into two macroscopically distinct glass phases, has a direct bearing on the conductivity threshold (Fig. 1). As alluded to above, we identify the low- $T_g$  glass phase with an Ag-rich phase. At a basic level, the specific heat increase near  $T_g$  when a glass melts provides a measure of the increased degree of freedom available in the molten state compared to the solid glass state. In the present case, the specific heat jump,  $\Delta C_p$ , provides a means to ascertain the degree of phase separation by directly relating it to the fraction of the two glass phases present. The volume fraction of the low- $T_g$  phase  $V(x)$ , deduced by analyzing the reversing heat flow signal, is vanishing at  $x < 7\%$ , but the fraction increases rapidly once  $x > 7\%$ . The fraction  $V(x)$  approaches the threshold value of  $\sim 1/6$  near a glass composition  $x = 9\%$  [Fig. 3(b)]. According to Scher and

Zallen [9], once the volume fraction of the minority (Ag-rich) phase acquires the threshold value of 16.6%, one expects that phase to percolate. A ternary glass at  $x > 9\%$  will be electrically shorted by the low- $T_g$  glass phase, and one expects the electrical conductivity to increase precipitously. Unfortunately, conductivity results in the critical region,  $8\% < x < 15\%$  are few and far between. The available results certainly suggest that a large jump in electrical conductivity is taking place once  $x > 10\%$ . Thus, a central finding of the present work is that a volume-percolation of the Ag-rich low- $T_g$  glass phase most likely contributes to the giant enhancement in electrical conductivity observed once  $x$  exceeds 10%.

#### E. Conductivity Threshold, Ag Tracer Diffusion, and Reversibility Window of the High- $T_g$ Phase

The molecular structure of the base  $\text{As}_2\text{S}_3$  glass has been the subject of numerous previous studies [12], [20]. The stoichiometric glass has often been modeled after its crystalline counterpart: orpiment ( $c - \text{As}_2\text{S}_3$ ) to consist of a fully polymerized network of S bridging pyramidal  $\text{As}(\text{S}_{1/2})_3$  units. If the picture were as simple as described above, one would expect  $\text{As}_2\text{S}_3$  glass to be nearly self-organized. Experiments have shown the stoichiometric glass to be stressed-rigid [24]. Detailed examination of Raman scattering [20] and Mössbauer spectroscopy [25] results show the glass in neither fully chemically ordered nor fully polymerized. Segregation of Realgar molecules clearly leaves the backbone S-rich. Alloying a few mole percent of  $\text{Ag}_2\text{S}$  in the base glass apparently lowers the connectedness of the backbone as glasses soften to enter the intermediate phase in the composition range  $8\% < x < 13\%$  (Fig. 2).

In analogy to earlier results on Chalcogenide glasses [15], [26], observation of the reversibility window permits fixing the *three elastic phases* of the high- $T_g$  phase. In the composition range  $9\% < x < 13\%$ , the majority phase present in the ternary glasses is the high- $T_g$  phase. Note that  $V(x) = 25\%$  at  $x = 10\%$  as shown from the plot of Fig. 3(b). The observation of a reversibility window suggests that glasses at  $x < 8\%$  are stressed-rigid, those at  $x > 13\%$  are *flexible*, while those in the *intermediate* composition are *self-organized* [18]. Thus, as the ternary glass composition increases to  $x = 13\%$ , the high- $T_g$  glass phase becomes elastically flexible. This has the important consequence that diffusion of  $\text{Ag}^+$  ions associated with the high- $T_g$  phase becomes facile, since the energy required to elastically deform the network and provide for the oversized  $\text{Ag}^+$  ion to diffuse decreases rapidly. Softening of the high- $T_g$  phase assists  $\text{Ag}^+$  ion conduction once  $x > 13\%$ , and also contributes to the conductivity enhancement observed in the present glasses in this composition range (Fig. 1).

Macroscopic segregation of the present ternary glasses in the  $8\% < x < 40\%$  range has some consequences for Ag tracer diffusion. One expects  $\text{Ag}^+$  ions to display two distinct diffusion constants, one associated with the high- $T_g$  phase and the other with the low- $T_g$  phase. The Ag diffusion in the high- $T_g$  phase would then be expected to increase dramatically as  $x$  exceeds  $x_c(2) = 13\%$ , and glasses enter the *flexible* phase. The available  $^{110}\text{Ag}$  tracer diffusion results of Drugov *et al.* [27] broadly support the picture above. Drugov *et al.* find Ag diffusion constant  $D = 5 \times 10^{-13} \text{cm}^2/\text{s}$  at  $x = 6\%$ , but to increase by nearly three orders of magnitude to  $D = 10^{-10} \text{cm}^2/\text{s}$  as  $x$  increases to 15%. Unfortunately, the group did not report Ag diffusion in

the region of interest, i.e.,  $6\% < x < 15\%$ , where large scale changes in conductivity are observed.

#### IV. CONCLUSION

The molecular structure of the ternary  $(\text{Ag}_2\text{S})_x(\text{As}_2\text{S}_3)_{1-x}$  glasses has been examined in MDSC and Raman scattering measurements over a wide composition range,  $0 < x < 70\%$ . At  $x > 7\%$ , glasses segregate on a macroscopic scale into an Ag-rich superionic-phase (low- $T_g$ ) and a semiconducting (high- $T_g$ ) phase. The present MDSC results show that the majority high  $T_g$  phase displays a reversibility window in the  $8\% < x < 13\%$  range. The observation fixes the three elastic phases in the glasses, with compositions at  $x < 8\%$  as *stressed-rigid*, those at  $x > 13\%$  as *flexible* while those in the intervening range,  $8\% < x < 13\%$ , belong to an *intermediate* phase [28]. The latter composition range comprises networks that are stress-free. The threshold behavior in electrical conductivity noted by Borisova *et al.* [1] near  $x \sim 10\%$  correlates well with: a) the present identification of the intermediate phase in the  $8\% < x < 13\%$  range (as illustrated in Fig. 1) and b) the macroscopic phase separation and subsequent volume percolation of the low  $T_g$  Ag-rich superionic-phase. Both features a) and b) are thought to contribute to the giant enhancement in electrical conductivity reported in the present ternary glasses.

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Authors' photographs and biographies not available at the time of publication.